# Reconstruction and Selection of Neutrino Interactions in MicroBooNE using Deep Convolutional Neural Networks MICROBOONE-NOTE-1123-PUB

The MicroBooNE Collaboration\*

Fermi National Accelerator Laboratory, Batavia, Illinois

# Abstract

In this document, we describe a new reconstruction workflow developed for the MicroBooNE experiment. It features the use of Deep Convolutional Neural Networks trained to recognize key structures within the data sufficient for the 3D reconstruction of neutrino interactions within the detector. As a test of the reconstruction utility, the products of the reconstruction workflow are used to select inclusive charged-current (CC)  $\nu_e$  and  $\nu_{\mu}$  interactions in both simulated and real MicroBooNE data. In simulation, our  $\nu_e$  and  $\nu_{\mu}$  selections achieve an efficiency of 57% and 68%, respectively, with a purity of 91% and 96%, respectively. We find that these selections are competitive with the inclusive selections used for the most recent MicroBooNE LEE searches. In particular, the CC- $\nu_e$  inclusive selection efficiency improves by over 20% while also improving sample purity. As a first step in quantifying potential bias, the data and Monte Carlo expectations are compared for both selections using the MicroBooNE open data. Within statistical and systematic uncertainties, both the electron and muon CC-inclusive event samples agree. A comparison of the real data events chosen by our work and another reconstruction framework shows that the two analyses each identify a sizeable fraction of events the other does not. This suggests that future analyses integrating the strengths of each could lead to combined gains. This work demonstrates, for the first time on real LArTPC data, state-of-the-art neutrino interaction reconstruction centered around deep learning algorithms.

<sup>\*</sup> MICROBOONE\_INFO@fnal.gov

# CONTENTS

I. Introduction	4
II. A CNN-based Neutrino Reconstruction for LArTPCs	5
A. Overview of the Reconstruction	5
1. Detector coordinate system and Data set terminology	9
B. LArMatch: 3D spacepoints and keypoints generation	10
1. Proposal of 3-wire intersections, or "triplets"	13
2. Feature Generating U-Net	15
3. Spacepoint real/ghost classifier	16
4. Spacepoint Keypoint score	17
5. Weighting the Multi-objective Loss	19
C. 3D Particle Trajectory Reconstruction	19
D. Keypoint Generation	20
E. Particle and Interaction Reconstruction with 3D Spacepoints	21
1. Forming track candidates	22
2. Forming shower candidates	24
F. Interaction Candidate Formation	28
G. Reconstruction Validation	29
1. Vertex Validation	30
2. Prong Validation	31
H. Energy Reconstruction	33
I. LArPID: A Prong Classification CNN	34
1. Network Inputs and Image Preprocessing	37
2. Network Architecture	39
3. Training	40
4. Network Performance	44
5. Interpreting the Model	46
III. Demonstration: Selection of inclusive $\nu_e CC$ and $\nu_\mu CC$ interactions in MicroBooNE	49
A. CC nue inclusive selection cuts	49
B. CC numu inclusive selection cuts	58

C. Systematic uncertainty estimates	60
1. Detector Systematic Uncertainties	61
2. Flux, Cross Section, and Hadron Re-Interaction Uncertainties	63
D. Results	65
E. Results of Data and MC comparison using Open Data Sample	70
IV. Discussion	71
V. Conclusions	76
References	78
A. Additional distributions for data vs expectation comparisons	82

### 1 I. INTRODUCTION

The liquid argon time projection chamber (LArTPC) is the detector technology of choice 2 for several future and current neutrino experiments. Current experiments include Micro-3 BooNE [1], the Short Baseline Neutrino Detector [2], and ICARUS [3]. Future experiments 4 notably include the Deep Underground Neutrino Experiment (DUNE) [4] an effort towards 5 which several prototype LArTPCs [5] have been constructed. LArTPCs have now found 6 their way into many experiments due to their combination of resolution and scalability. 7 LATTPCs can track charged particle trajectories with millimeter-scale position resolution 8 for detectors with target volumes into the tens of kilotons. 9

The output of LArTPCs can be characterized as very image-like. The waveforms recorded 10 from planes of sense wires can be naturally arranged to produce images of the ionization 11 patterns left behind by charged particles traversing the detector. Image formats are also 12 relevant for alternative readout designs for LArTPCs, such as those that directly measure 13 the 2D location of ionization in order to naturally capture voxelized 3D trajectories [6]. The 14 format of this spatial data has facilitated the application of newly developed machine learning 15 techniques, in particular from the domain of computer vision, to the task of reconstructing 16 the trajectories and particle interactions captured by LArTPCs. Early applications focused 17 on the classification of either entire images cropped from the data or for individual pixels [7]. 18 Structures traditionally important in the reconstruction of interactions, such as the location 19 of neutrino vertices have been searched for. High-level, more abstract quantities such as 20 neutrino interaction flavor [8], the energy of electromagnetic (EM) showers [9], and the 21 neutrino energy [10] have been targets of ML algorithms. While these applications were on 22 2D image data, there has been much progress in developing a full reconstruction chain for 23 3D voxelized data. 24

A fully end-to-end machine learning workflow outputs pixel-wise particle classification, the location of key points on particle trajectories, particle clusters, and assembled neutrino interactions into a fully-differentiable workflow [11]. The application of ML to reconstruction has indeed seen rapid progress in the past several years. However, demonstrations of these ML-based tools in the context of analyses of real LArTPC data are only starting to be realized. One such analysis centered around a CNN performing pixel-wise particle-type classification [12, 13] which was used as a central input for the targeted exclusive selection of one-lepton and one-proton final state interactions [14]. This analysis was part of MicroBooNE's search for an excess of low-energy electron neutrino interactions [15], conducted to
investigate the reported event excess observed by the MiniBooNE experiment [16].

This document provides a description of a new "DLGen2" reconstruction and applies it to 35 the selection of inclusive  $\nu_e CC$  and  $\nu_\mu CC$  interactions in MicroBooNE. Unlike the previous 36 MicroBooNE DL-based analysis, this iteration has aimed for the general reconstruction of 37 all charged particle trajectories coming from neutrino interactions. An overall evaluation 38 and demonstration of the reconstruction is conducted through the execution of the selection 39 on the MicroBooNE open neutrino data set. We find that the efficiencies for this analysis 40 are competitive with the highest-efficiency search previously published by MicroBooNE [17], 41 which utilizes the Wire-Cell reconstruction [17–19]. Furthermore, the inspection of events 42 selected by our reconstruction finds unique events not found by the analysis of Ref. [17]. 43

# 44 II. A CNN-BASED NEUTRINO RECONSTRUCTION FOR LARTPCS

# 45 A. Overview of the Reconstruction

The reconstruction utilizes convolutional neural networks to enable both 3D energy deposit reconstruction and perform particle ID on 2D images. The approach taken makes use of the different advantages inherent in the 2D image and 3D point cloud representations. We start the description of the reconstruction chain with a brief overview of the major components of the reconstruction, which are illustrated in figure 1. Later sections then will describe the algorithms used in each component in more detail.

The input to the reconstruction is a set of three 2D images, one for each of the wire-52 planes installed inside the MicroBooNE liquid argon TPC (LArTPC) detector [1]. The 53 waveforms arranged in these images are the output of the first pre-processing stage applied 54 to the raw waveforms. This stage includes the removal of coherent noise seen in sets of 55 neighboring channels [20]. It also reconstructs the original space charge distribution from 56 the measurements on wires by reverting the detector response (e.g., electronic response and 57 field response) and sparsifying the input images. We call this process "Signal Processing." 58 For more details on the pre-processing stage see Refs. [21, 22]. 59

<sup>60</sup> The image set is then provided to two convolutional neural networks (CNN). The first



Figure 1: Overview of the reconstruction workflow. The wireplane images and optical information are passed into several components to produce labeled spacepoints reconstructing the location of ionization left behind by charged particles traversing the LArTPC. The labels associated to each spacepoint include particle type and a tag estimating if a given spacepoint is from beam-related or cosmic-ray particles. These points are then clustered into candidate particle trajectories by a set of reconstruction algorithms. A CNN is used to provide a particle-type label for each trajectory. The final output of the workflow are candidate neutrino interactions formed by associating one or more particle clusters to neutrino vertex candidates.

CNN acts on each wire plane image separately and is responsible for labeling each pixel 61 in the image according to two broad particle categories, split by the spatial pattern of 62 ionization produced. The first type is "track"-like trajectories coming from particles such 63 as muons, charged pions, and protons. The second type is "shower"-trajectories produced 64 by electromagnetic cascades initiated by electrons or photons interacting in the detector. 65 This pixel labeling CNN is referred to as "SSNet" for the semantic-segmentation network 66 and was used in the first MicroBooNE DL analysis. The details of SSNet can be found in 67 Ref. [13]. 68

A second, new CNN is applied to the set of three 2D images collectively and is referred to as the "LArMatch" network. The network produces two outputs. The first is a set of candidate 3D spacepoints which represent the location of energy depositions consistent with input images. The second product is a set of scores for six different classes of "keypoints." Keypoints are useful locations at the start or end of tracks and showers, which, if known, can greatly simplify the algorithms required to help with clustering and the formation of neutrino <sup>75</sup> interaction candidates. The keypoint classes consist of 1) potential neutrino interaction
<sup>76</sup> vertices, 2) the start of track-like particles, 3) the end of track-like particles, 4) start points
<sup>77</sup> of EM showers excluding those from delta rays and muon decay, (5) the start points of delta
<sup>78</sup> ray showers, and 6) the start point of showers from muon decay.

The input images also go through a reconstruction workflow separate from the one de-79 scribed here. This workflow, referred to as the "Wire-Cell" reconstruction [18], builds space-80 points, does clustering, and matches clusters of charge to pulses of light seen in the optical 81 detectors [19]. The workflow uses many non-ML approaches and features the application 82 of compressed sensing. What we utilize in our reconstruction workflow is the association of 83 charge clusters to pulses of light either inside or outside the neutrino beam window. This 84 information is used to provide a tag for the spacepoints made by the LArMatch network, as 85 either in-time or out-of-time with the neutrino beam. 86

At this point in the reconstruction, we have a set of spacepoints with various tags deriving 87 from pixel-based labels along with a collection of keypoints. The next step in the workflow is 88 to reconstruct 3D spacepoints, which are then clustered into subclusters covering individual 89 particle trajectories. The purpose of starting with subclusters is to emphasize the purity 90 of the clustering over completeness. Here the purity refers to the largest fraction of points 91 whose ground truth label is associated to the end of the event. A pure cluster would contain 92 spacepoints associated to only one particle. The completeness measures the fraction of 93 possible pixels or spacepoints in the cluster. 94

The 3D clustering algorithm implements the commonly used Density-Based Scan (DB-95 Scan) algorithm which uses the distances between k-nearest neighbors. What allows for this 96 simple clustering routine is the many tags coming from LArMatch, SSNet, and the Wire-97 Cell in-time/out-of-time algorithm. These labels are used to partition the spacepoints before 98 clustering, helping to reduce overclustering where spacepoints from two different particle tra-99 jectories are included into one cluster. For example, the LArMatch track and shower start 100 keypoints are used to temporarily remove nearby spacepoints in order to prevent spacepoints 101 from particles coming out of a common interaction vertex from being grouped together. 102

After the subclustering step, non-ML algorithms are then used to combine the subclusters to form sets of spacepoints intended to represent the ionization produced by a single particle. These algorithms make use of the LArMatch ouputs for track endpoints and shower starts to seed the particle-building algorithms. After this clustering stage is complete, the reconstruction has formed candidate particle trajectories. The following stage forms neutrino interaction candidates by associating primary particle trajectories to interaction vertices. Secondary trajectories are also associated to interactions by looking for trajectories that seem to emerge from previously included trajectories. Cosmic muon trajectories are also formed by using track start and end keypoints to seed the track-building algorithm applied to only out-of-time subclusters. Neutrino and cosmic muon candidates are the core outputs of the 3D reconstruction workflow.

For the individual neutrino interactions, further analyses are performed. Another CNN, 114 referred to as "LArPID", assigns particle identification scores to individual particle trajecto-115 ries. This LArPID network acts on two sets of images for a given individual particle cluster. 116 The first set of images are sub-images formed by cropping around the cluster's projected 117 position on each wire plane image. These images include values for only those pixels at 118 the projected locations of spacepoints. The second set of images provided to LArPID is a 119 set of "context" images which use the same cropped location but include more pixels, only 120 masking out pixels with an out-of-time tag (those likely not produced by interactions asso-121 ciated with the beam). The purpose is to provide LArPID with both a given cluster's pixels 122 and information pertaining to the entire interaction. We believe (see section III5) that the 123 context images are critical in maximizing the particle ID accuracy of LArPID. The context 124 images provide information the network can use to better ID the cluster. The context im-125 ages also provide the means to overcome clustering errors from the 3D spacepoint algorithms 126 by providing information that might have been lost during clustering but is still present in 127 the images around the location of the clusters. The primary output of LArPID is particle 128 class scores for five particles: muon, charged pion, proton, electron, and photon. Particles 129 and their anti-particles are combined into the same class. LAPID also provides auxiliary 130 outputs in order to provide the option to make data selection cuts based on estimates of 131 the cluster reconstruction quality and as to whether the particle in question is a primary 132 particle emerging from a neutrino interaction vertex or a secondary particle descended from 133 the interactions of the primary particles. 134

The final outputs provided by the reconstruction are collections of candidate neutrino interactions and cosmic muons. For each neutrino candidate, each prong (reconstructed track or shower cluster) is provided a particle ID score from LArPID. Using this network's ID, the energy and 3-momentum are estimated for each particle. The kinematics estimator for muons, protons, and charged pions is based on the visible tracklength and uses the relationship between particle energy and the estimated length of fully ranged-out particles.<sup>1</sup> The energy estimator for the electromagnetic showers uses calorimetry based on charge. Additional network outputs related to keypoint scores and LArPID estimates are also passed along as outputs. The information for candidate neutrino interactions and their constituents can then be used to develop physics analyses.

In the rest of this section, we provide more details for a subset of the components discussed above. We do not include discussions of the image pre-processing algorithms, the in-time/out-of-time Wire-Cell tagger, and the SSNet CNN since their details can be found in the indicated references. For each component described, we focus on outlining the core approach of the algorithms, reference previous related work, and document key heuristics in tuning their behaviors.

# 151 1. Detector coordinate system and Data set terminology

We will often visualize the outputs of the reconstruction or define performance metrics 152 assuming a specific 3D coordinate system. For the basis vectors, the positive  $\hat{x}$ -direction 153 runs in the direction of the anode to the cathode and points in the direction opposite to the 154 drift of ionization electrons towards the anode. The positive  $\hat{z}$ -direction runs in the same 155 direction of the neutrino beam. The positive  $\hat{y}$ -direction points upward to the sky. The 156 origin of the coordinate system is defined at the boundary of the TPC where z = 0 is the 157 side closest to the source of the beam, i.e. upstream, x = 0 is at the induction plane closest 158 to the drift volume, and y = 0 is located at the midpoint of the vertical TPC dimension. 159 The MicroBooNE TPC is a rectangle whose lengths are (256 cm, 233 cm, and 1036 cm) 160 along the (x, y, z) axes, respectively. 161

Another important definition is what constitutes an "event". The values specified here are particular to the MicroBooNE experiment. However, the overall data schema will be similar for other LArTPCs utilizing sense-wires. Each event includes a set of waveforms from each of the three wire planes that are arranged in a 2D array to make three wire plane images, which we will refer to as "TPC images" or simple "images." The three wire planes of the MicroBooNE detector – from closest to the TPC drift region to the furthest – are

<sup>&</sup>lt;sup>1</sup> This estimate is applied to tracks regardless of whether they range out inside or exit the detector. A more accurate estimate for exiting tracks will be the subject of future work.

the first induction plane, the second induction plane, and the collection plane. They are so-named by the process with which ionization produces a current signal within the sense wires. The three wire planes are given a label, 'U', 'V', and 'Y', respectively. Every event will have exactly one TPC image from each of the three planes.

Each of the waveforms that makes up the images in an event consists of a time series 172 of 9600 voltage measurements, or samples, recorded every 0.5 microseconds. The primary 173 DAQ system for the MicroBooNE detector must be externally triggered (in other words 174 instructed) to capture a synchronous set of waveforms for all channels. The two trigger 175 types relevant for this work include (1) a signal synchronized with a firing of the neutrino 176 beam, typically referred to as a "spill" (which references the release of a bunch of protons 177 from the accelerator into a carbon target), and (2) a trigger signal produced by a signal 178 generator programmed to fire at regular intervals in a time window between beam spills. 179 The data recorded using the latter, non-beam spill, triggers are referred to as the "externally 180 triggered" or EXT data set. The MicroBooNE detector records waveforms in sync with the 181 Booster Neutrino Beam (BNB) produced by Fermi National Laboratory, and the data set 182 recorded in coincident with the firing of this beam is referred to as the "BNB" data. Later 183 in the sections demonstrating the performance of the reconstruction workflow through its 184 use in a neutrino event selection, only data from the BNB and EXT data sets are used. 185

### B. LArMatch: 3D spacepoints and keypoints generation

The purpose of the LArMatch network, illustrated in figure 2, is to use the TPC wire plane 187 images to infer information related to the 3D location of ionization made by charged particle 188 trajectories. Inferring the true location of such ionization is not trivial as this essentially 189 requires inverting a tomographic projection, which by its nature will be an under-specified 190 problem due to the information lost during the projection operation. To make this difficulty 191 more concrete, we can consider trying to infer the location of energy depositions coming from 192 a uniform line of ionization where the line is parallel to the wire readout planes. Figure 3 193 provides an illustration showing the signal that would be seen in the wire plane images, 194 which is simply a line of uniform intensity across some set of wires all occurring at the same 195 time (i.e. region of TPC samples). A naive approach would be to ask "what is the set 196 of spacepoints that is consistent with producing a wire signal in all three planes?". This 197



Figure 2: LArMatch network schematic. First, a U-Net CNN with residual convolutions takes as input three TPC images. For each input pixel, the CNN outputs a (16-dimensional) vector whose purpose is to represent the relevant patterns around a given pixel. Next, a non-ML algorithm proposes candidate spacepoints by forming all possible locations consistent with the charge deposition pattern in the images. The location of each proposed spacepoint is projected into the wire plane images in order to associate it a pixel from each wire plane. A (48-dimensional) feature vector for each spacepoint is made by concatenating the feature vectors belonging to the associated pixels. Three sets of multi-layer perceptrons (MLPs) then map the spacepoint vector to three types of outputs. One output is the score determining if a proposed spacepoint is located where a true energy deposition occurred. The second is a score for five particle types. The other output is a score indicating the location of several types of keypoints.

defines a 2D region of possible spacepoints, indicated by the purple region in the bottom 198 illustration of Figure 3. The true locations of ionization would occur along a line within this 199 region, indicated by the dashed line in the figure. One can select a subset of spacepoints in 200 this region by utilizing some physical priors. If one assumes prior knowledge that (1) the 201 true trajectory comes from a line segment and (2) the ends of the line must be consistent 202 across the planes, then the set of possible spacepoints reduces to the correct region around 203 the true path of ionization, as indicated by the yellow regions in the illustration of Figure 3. 204 Another important refinement is to enforce some consistency in the signal intensity between 205 the planes. In our example, one can use what in principle should be differences between the 206 planes for the intensity per wire due to the different projected lengths of the ionization path 207 onto the region around each wire. One can also impose a regularizing constraint such as 208 biasing towards solutions that minimizes the number of spacepoints, which in this example 209



Figure 3: Example illustration of how inferring the 3D location of ionization can be an under-specified problem. We assume a line of uniformly distributed ionization occurs within the TPC and that the line is parallel to the wire planes. In this case, the wire plane images (top row) will contain a line of signal (cyan) occurring at the same time. Using only the knowledge of which wires on the planes see a signal, there is a 2D region in the TPC of possible spacepoints that are consistent with the wire plane signals (shown in purple). Only by also assuming a line shape and testing for consistency of the line length across planes can one determine the true region of ionization (shown in yellow) that corresponds to the true path.

can be seen to have a similar effect to having a line-like prior. These two latter approaches are a core part of the approach employed by the Wire-Cell reconstruction framework [18]. What this example is meant to illustrate is the type of prior information or strategies needed to pick out the true points of ionization. While this example is the worst-case scenario for simple line trajectories, for LArTPC wire planes on the surface or in regions with many particles emerging from a neutrino interaction other degeneracies will arise.

The motivation for the LArMatch network is to complement charge consistency and reg-217 ularization by using machine learning to find additional features to match across the planes 218 which improves the identification of true ionization points. One can imagine separating true 219 3D energy depositions from false ones by learning to "match" local energy deposition pat-220 terns in one plane to another. These patterns must follow coherently from the underlying 221 3D patterns of ionization. The algorithm thus proceeds in two steps. The first is to use a 222 simple, deterministic algorithm to propose a large set of possible 3-wire intersections that 223 might correspond to the location of real energy depositions in the detector. Next, a convo-224 lutional neural network (CNN) is trained to identify which 3-wire intersections are real or 225

false. We use what is known as a 'U-Net' for the CNN architecture. A U-Net maps the input 226 images to a set of latent vectors at each pixel whose purpose is to summarize the relevant 227 information in the neighborhood of the pixel. For a given 3D spacepoint, we project its 228 location onto each wire plane and associate a pixel from each. We then concatenate the 229 feature vectors from each pixel and pass them to a multi-layer perceptron which outputs a 230 score indicating if the spacepoint is real or false. The feature vectors are also used by other 231 MLP heads to produce additional information. In total, each feature vector is mapped to 232 three outputs: (1) a score indicating if the spacepoint is true or false, (2) a set of scores 233 classifying the spacepoint as one of five particle types, and (3) a set of scores related to how 234 far away the point is from five types of keypoints. In the following sections, we first describe 235 the algorithm that produces the spacepoint proposals from the wire plane images. We then 236 provide details on the image-to-feature vector U-Net. Finally, we discuss the three different 237 output heads. 238

# 239 1. Proposal of 3-wire intersections, or "triplets"

The first step to the LArMatch approach is to generate spacepoint candidates simply 240 based on minimal geometric plausibility. Initial spacepoints represent the location of 3-wire 241 intersections for wires with an above threshold signal coincident in time. We represent these 242 wire combinations as a "triplet" of integers whose components contain the index associated 243 with wires from each of the three wire planes. When the wire plane data is represented as 244 an image, the triplet refers to the tuple of column indices for the three wire plane images. In 245 order to not miss spacepoints that project onto non-responsive wires, the wire combinations 246 can include one wire which has been tagged as non-responsive. About 10% of the sense wires 247 in the MicroBooNE detector are classified as non-responsive. We do not try to make up for 248 missing spacepoints due to below threshold wire signals caused by ionization patterns that 249 cause destructive interference on the induction wires. These are associated with ionization 250 patterns where local segments are perpendicular to the wire planes. False positive and false 251 negative errors can also be induced by the presence of noise features on the wires. 252

We form a set of candidate triplets for each time tick (represented by a row in the 2D wire-plane images) in the wire plane signals. The three column indices and row index specify the projected pixel locations in the three wire planes. This information also specifies a 3D location determined by (1) the location of the 3-wire intersection and (2) knowledge of
which image row represents the time coincident with the beam trigger combined with a drift
velocity assuming a perfectly uniform drift field.

The proposed spacepoints for an example simulated MicroBooNE event are shown in 259 Figure 4. Metadata, which captures the "truth" about the particle trajectories present in 260 each event, is saved during the simulation and used to create the ground truth labels for the 261 LArMatch network. This includes both a list of charged particle trajectories passing through 262 the TPC and the location of energy deposited by the particles. To save disk space, much of 263 this information is projected into an 2D array with the same dimensions as the wire plane 264 images, thereby facilitating the ability to determine the particle type or individual trajectory 265 ID that deposited the most ionization observed at a given 2D pixel. In the simulation, the 266 locations where energy was deposited by a particle is stored. For each pixel in the wire plane 267 image, we assign to it the largest energy deposition that contributed to the value in the pixel. 268 We then project this position into the other wire planes. The pixels on the other wire planes 269 then are used to calculate the shift in the number of columns between the pixels on the 270 two wire planes. In order to recover the YZ location of the largest energy deposit cluster 271 that contributed to the pixel in the starting plane, one calculates the 2D intersection of the 272 two wires from the different planes. The distance of the energy deposit from the wire plane 273 can be calculated from the time relative to the event trigger and the drift velocity. Given 274 that the wire planes are a tomographic projection of the 3D space points, this method of 275 saving the 3D locations does not allow for perfect inference. However, we find the accuracy 276 is sufficient to construct the ground truth for the LArMatch network, while reducing the 277 amount of data to be saved. For future work, it would be worth exploring a better method 278 of compressing the 3D energy deposition information that is not inherently lossy. 279

In figure 4, the proposed spacepoints for one event are shown along with the ground 280 truth 'true' or 'ghost' labels built from the simulation metadata. Spacepoints near a true 281 location of ionization are given the 'true" ground truth label shown in red. The rest of the 282 spacepoint proposals are given the 'false' ground truth label shown in blue. We highlight 283 two regions of this figure. The first is the volume between z = [600 cm, 800 cm]. Here, many 284 short line-like regions of false spacepoints are seen. This is due to a fairly large region of 285 unresponsive wires on one of the wire planes (the "Y" collection plane). In these regions, the 286 requirement to propose a spacepoint is relaxed from requiring ionization to be observed on 287



Figure 4: Initial spacepoint candidates for an example simulated MicroBooNE event. The "true" spacepoints located near regions of ionization are colored in red. The "false" or "ghost" spacepoints that are not near ionization are colored in blue.

only two (as opposed to all three) wire plane images. We make this accommodation with the aim of minimizing the amount of missing ionization at the cost of potentially accepting more false positives. The idea will be to use a downstream algorithm, specifically a particle-level CNN, to correct for false spacepoints or clustering mistake. The other region to point out in Figure 4 is the relatively large region of false (i.e. blue points) surrounding one muon track between z=[400 cm, 600 cm]. This is where a portion of a cosmic muon is parallel to the wire planes, similar to the illustration discussed earlier.

#### 295 2. Feature Generating U-Net

The core part of the LArMatch network is the U-Net [23] CNN mapping images to pixel-296 wise feature vectors. We use residual convolutions [24] over standard convolutions. There are 297 a total of six convolutional layers including five downsampling layers, each time with stride 298 two. When normalization layers are used, we use instance normalization [25]. We upsample 299 on the decoder part of the network with convolution-transpose operations. Because the wire 300 plane images are sparse, i.e. most pixels have a value very nearly zero, the network uses 301 sparse-submanifold convolutions [26] as implemented by the MinkowskiEngine library [27]. 302 The U-Net takes in a sparse tensor representation of a single wire plane image at a time 303

and is applied to each wire plane, separately. In other words, the input of the U-Net is a 304 sparse tensor, s, which consists of a list of N pixels, which is a subset of all the pixels in the 305 image. To be included into the sparse tensor, a pixel had to pass two criteria. One was that 306 the pixel had a value above some threshold value. We used a threshold of  $\geq 10.0$ , or what 307 is about a quarter of the average pixel value for minimum ionization sections from cosmic 308 muon tracks. The second criterion is that a pixel, with a below threshold value, was from a 309 non-responsive wire while also being the projected location of a proposed spacepoint. The 310 sparse image tensor,  $\mathbf{s}$ , is represented through a pair of tensors. The first is a coordinate 311 tensor,  $\mathbf{c} \in \mathbb{W}^{N \times 2}$ , which contains the indices of the above threshold pixels. The second is 312 a feature tensor,  $\mathbf{f} \in \mathbb{R}^{N \times 1}$ , containing the associated pixel values. The U-Net, therefore, 313 maps  $\mathbf{s} = (\mathbf{c}, \mathbf{f})$  to N 16-dimensional feature vectors,  $\mathbf{v} \in \mathbb{R}^{N \times 16}$ . 314

### 315 3. Spacepoint real/ghost classifier

A 2-layer MLP is used to classify each proposed spacepoint as either real or ghost. This classifier takes in the concatenated 48-dim feature vector,  $\vec{v}$ , formed from the individual 16-d feature vectors from the project pixels from each plane. The MLP has two hidden layers, each with 32-features, and outputs both a real and ghost class score. A softmax function normalizes the sum of these scores to 1.0. We use the normalized score for being a true spacepoint,  $p(\vec{v})$ , for classifying proposed spacepoints.

We train the network to optimize this prediction using a focal loss [28] objective. We also weight each spacepoint based on the relative total number of ground truth-labeled real and ghost points. This weighting is used to mitigate bias that might favor true negative predictions coming from the higher frequency of ghost spacepoints compared to real spacepoints. Our training objective is

$$\min_{\theta} \mathcal{L}_{ghost} = \min_{\theta} \left[ \sum_{b}^{N_{b}} \left[ \sum_{i_{t}}^{N_{i_{t,b}}} w_{b,t} \log(p_{\theta}(v_{i,t}))(1 - p_{\theta}(v_{i,t}))^{\gamma} + \sum_{i_{f}}^{N_{i_{f},b}} w_{b,f} \log(1 - p_{\theta}(v_{i,f}))(p_{\theta}(v_{i,f}))^{\gamma} \right] \right].$$
(1)

<sup>327</sup> We optimize the objective using AdamW, an implementation of stochastic gradient descent

with features such as adaptive gradient normalization and momentum. We train our models 328 with randomly sampled batches of data. The parameters of both the UNet and the MLP 329 heads producing the LArMatch outputs are learned simultaneously in one combined training 330 procedure. Within a batch of  $N_b$  training samples, the b-th sample consists of  $N_b$  feature 331 vectors,  $v_i$  produced by the UNet for all  $N_b$  candidate spacepoints. We use the simulation 332 meta-data to produce ground truth labels for the set of vectors,  $v_i$ . The subset of  $N_{b,t}$ 333 'real' or 'true' ground truth-labeled vectors is  $v_{i,t}$ ; the subset of  $N_{b,f}$  'ghost' or 'false' labeled 334 vectors is  $v_{i,f}$  (with  $N_b = N_{b,t} + N_{b,f}$ ). The likelihood estimate for being a real point is 335  $p_{\theta}(v_i)$  and is approximated by the output of the true/ghost MLP, parameterized by  $\theta$ . The 336  $(1-p_{\theta}(v_{i,t}))^{\gamma}$  and  $(p_{\theta}(v_{i,f}))^{\gamma}$  are the focal-loss factors. As  $p_{\theta}(v)$  approaches the ground truth 337 value (1.0 for real points, 0.0 for ghost points), the focal loss factors increasingly down-weight 338 these examples with the  $\gamma$  meta-parameter controlling how quickly the downweighting occurs 339 with increased confidence. Conversely, the spacepoints whose classification is incorrect will 340 contribute more to the update of the model parameters. In effect, the focal loss is intended to 341 nudge the optimization towards improving "harder" examples over increasing the confidence 342 for easy examples. 343

#### 344 4. Spacepoint Keypoint score

The LArMatch network also is tasked with providing the outputs to identify locations of ionization that can be useful for later 3D trajectory reconstruction. We defined six classes of "keypoints": (1) a neutrino interaction vertex, (2) the start of a track-like trajectory (defined as belonging to a muon, proton, charged pion, and other heavy mesons), (3) the end of a track-like trajectory, (4) the start of EM shower not produced by processes in the following types, (5) the start of EM showers produced by the decay of a muon, and (6) the start of EM showers form delta rays (typically radiating from energetic muon tracks).

The way the location of possible keypoints is represented in the output of the network is through a score made for each spacepoint. The score ranges from 0 to 1.0, with scores inversely proportional to the distance to a keypoint. The network is trained to reproduce a score distribution that follows a Gaussian with a uniform, uncorrelated variance. In other words, the network is asked to produce a heat map near keypoints with the hotspots having a set shape. A post-processing step can then be used to identify hotspots and use the spatial score distribution to fit to the precise keypoint location. The ground truth-score is calculated using meta-data from the simulation which retains the creation point of charged track-like particles and the earliest location of ionization within the TPC of an EM shower. All particles whose meta-data information was used to define EM shower keypoints were required to have at least one wireplane image with 20 or more pixels whose signal was attributed to its ionization.

<sup>364</sup> A 2-layer MLP,  $s_{\theta}$  is used to map each spacepoint's feature vector,  $\vec{v}$ , to a vector,  $\vec{k} \in \mathcal{R}^6$ , <sup>365</sup> whose components are the scores of each keypoint class. The value of each component is <sup>366</sup> independently kept within the range of [0, 1] by applying a sigmoid-function element-wise. <sup>367</sup> This bounded output is then compared to the ground truth scores for each keypoint class.

Both the dedicated keypoint MLP and the UNet parameters are optimized to minimize the keypoint training objective,  $\mathcal{L}_{keypoint}$ , given by

$$\mathcal{L}_{keypoint} = \frac{1}{N_b} \sum_{b}^{N_b} \left[ \frac{1}{N_c} \sum_{c}^{N_c} \left[ \sum_{i}^{N_{b,t}} w_{b,c,t} (\hat{s}_{i,c,b,t} - s_{\theta}(\vec{v}_{i,b,t}))^2 + \sum_{j}^{N_{b,f}} w_{b,c,f} (\hat{s}_{j,c,b,f} - s_{\theta}(\vec{v}_{j,b,f}))^2 \right] \right].$$
(2)

For the above equation, the sum over  $N_b$  is over the number of examples in each training 370 batch. Each example consists of proposals from one set of wire plane images from one TPC 371 readout event. The sum over  $N_c$  is over the six different keypoint classes. Because most 372 spacepoint proposals are unlikely to be near a true keypoint, to aid training, we use weights 373 to balance the contribution of examples near true keypoints, for which the MLP needs to 374 output a score, and those far away from true keypoints, for which the MLP only needs to 375 output zero. Therefore, for each class we split the total number of spacepoint proposals in 376 the b-th example,  $N_b$ , into "true example" points within 10 cm of a true keypoint and "false 377 example" points which are not. Thus, in the above equation, the sum over  $N_{b,c,t}$  is for the 378 true example spacepoints for class c, while the sum over  $N_{b,c,f}$  for the false examples for 379 class c within the b-th example of the batch. Regardless of the class, the number of true and 380 false examples total to the same number of spacepoint proposals, i.e.  $N_{b,c,t} + N_{b,c,f}$ . The 381 true example weight for class  $c, w_{b,c,t}$ , is set to the ratio of the total number of spacepoints, 382  $N_{b,c,t} + N_{b,c,f}$ , over the number of true examples in the b-th training example. Similarly, 383

the weight,  $w_{b,c,t}$ , is the ratio of the total number of spacepoints over the number of false examples in the *b*-th training example. For each true (false) spacepoint, the contribution to the loss is the weighted squared-difference between the keypoint MLP output,  $s_{\theta}(\vec{v}_{i,b,t})$  $(s_{\theta}(\vec{v}_{j,b,f}))$ , which is a function of the feature vector,  $\vec{v}_{i,b,t}$  ( $\vec{v}_{j,b,f}$ ), of the *i*-th (*j*-th) spacepoint in the *b*-th training example. The ground truth score for a given spacepoint is labeled by  $\hat{s}_{i,c,b,t}$  and  $\hat{s}_{i,c,b,f}$ .

#### 390 5. Weighting the Multi-objective Loss

We use a dynamic weighting of the different task objectives when forming the final, overall loss function. This technique changes the relative weights of the tasks based on an estimate of the uncertainty. This method in effect aims to encourage parity in the contribution of the terms to the total loss throughout the training period. In our application, the total loss is

$$\mathcal{L}_{larmatch} = e^{-s_{ghost}} \mathcal{L}_{ghost} + e^{-s_{keypoint}} \mathcal{L}_{keypoint} + s_{ghost} + s_{keypoint}.$$
 (3)

### <sup>395</sup> C. 3D Particle Trajectory Reconstruction

The 3D reconstruction of individual particle trajectories is designed around the outputs 396 produced by the LArMatch CNN, the SSNet CNN, and the Wire-Cell out-of-time tagger. 397 The fundamental input to the reconstruction is the set of spacepoints produced by the 398 LArMatch stage. The algorithms described below first create clusters belonging to individual 399 particles. This is followed by building a representation of the trajectory. A line segment, fit 400 to a cluster's spacepoints, is used to represent track-like particles. A cone, whose axis is fit 401 along an initial path of spacepoints, represents shower-inducing particles. These outputs are 402 more easily achieved by the pattern recognition performed by the previous CNNs, alleviating 403 the need to find the necessary patterns within the set of spacepoints, directly. 404

The upstream outputs are first used to refine and partition the candidate spacepoints. First, the LArMatch real/ghost score is used to filter ghost points. A 'real' spacepoint score threshold of 0.8 is applied to remove ghost points. This score value removes approximately 90% of ghost points and keeps approximately 75% of true points. The cut value chosen favors background rejection in order to keep the typical run time of downstream algorithms between

10-20 seconds per event. Next, the Wire-Cell out-of-time/in-time label splits the spacepoints 410 into two sets: 'in-time' and 'cosmic'. Both of these sets are subdivided into track and shower 411 hits using the scores from the 2D SSNet CNN. At this stage of the reconstruction, we have 412 four buckets of spacepoints: in-time-track, in-time-shower, cosmic-track, and cosmic-shower. 413 Because of spacepoint proposal's very forgiving criteria, the density of points around the 414 true trajectory can be high with many spacepoints providing redundant information. We 415 apply a heuristic to remove points away from the core of the trajectory. For each plane, we 416 only tag one spacepoint to keep per pixel, choosing the spacepoint with the largest LArMatch 417 real/ghost score. The final set of spacepoints we keep are the union of all the spacepoints 418 associated with pixels from each plane. This heuristic is applied to the in-time-track, in-time-419 shower, and cosmic-track spacepoint partitions. Figure 5 shows the fraction of space points 420 that are within some distance of a true muon, charged pion, or proton trajectory within the 421 TPC. The simulated data used to make the plot in this figure contained simulated cosmic 422 particles (mostly muons) and neutrino interactions. About 90% of spacepoints are within 1 423 cm of track-like trajectories. 424



Figure 5: Fraction of spacepoints vs. distance from the ground truth trajectory of a true muon, charged pion, or proton trajectory within the TPC.

# 427 D. Keypoint Generation

The output of the LArMatch keypoint proposal CNN are pixel-wise scores. This information needs to be distilled into individual keypoint candidates. Ideally, the scores from

the network should be arranged spatially as spherical hotspots. We separate the hotspots 430 by first retaining keypoints with a minimum score and then using density-based clustering 431 algorithm, DBSCAN, to identify individual candidates. The location of a keypoint is taken 432 to be the spacepoint within a cluster with the highest keypoint score. Spacepoints part of a 433 reconstructed keypoint are tagged and removed from the original pool. The scores of points 434 within the remaining pool are modified by using the set of newly created keypoint locations 435 to subtract the expected score contributions (defined by a Gaussian function). The modified 436 score is clamped to be zero or greater. This keypoint-finding procedure is applied twice, first 437 with a high keypoint score threshold and again with a lower score threshold. This procedure 438 is applied separately for each type of keypoint. As a result, a spacepoint can be a part 439 of keypoint clusters for multiple classes. However, a spacepoint can only be part of one 440 keypoint cluster within the same class. 441

Keypoints from all six classes are searched for within the 'in-time' spacepoint partition. Only track-start and track-end types are constructed from the 'out-of-time' spacepoint partition. All of the above keypoints will be used by the next set of algorithms to seed the creation of particle clusters.

In the future, keypoints with the remaining classes can be built using the out-of-time spacepoints. This could be used to reconstruct cosmogenic particle clusters, beyond those for cosmic muons, with the intended use of creating side-band datasets. For example, it might be useful to reconstruct out-of-time neutron-induced interactions. These could be identified by track-start keypoints or regions with high neutrino-like scores as they often mimic NC-like final states.

#### 452 E. Particle and Interaction Reconstruction with 3D Spacepoints

Two different sets of algorithms are used to form track-like and shower-like clusters. However, both take the approach of trying to form pure sub-clusters and then using heuristics to stitch together the subclusters belonging to individual particles.



Figure 6: Schematics of the steps of the track reconstruction. (A) Spacepoints with track-like and in-time labels are collected along with start and end keypoints (here a start keypoint is shown in cyan; end keypoints are in magenta). (B) Spacepoints around certain keypoints are removed from clustering. (C) Spacepoints are clustered and then broken into straight pieces based on the convex hull around the points. (D) Clusters are represented as a line segment with two ends. Line segments between end points within a certain distance are formed. A graph is defined with nodes defined by the cluster end points and two types of edges defined by the line segments within charge clusters (black solid lines) and those between clusters (red dashed lines). (E) Track-start keypoints are used to seed a depth-first graph traversal algorithm that proposes possible tracks. (F) Spacepoints are assigned to nearby line-segments and together define a candidate particle track. In this schematic, four candidates are proposed.

#### 456 1. Forming track candidates

For track-like particles, we form subclusters by looking for neighboring spacepoints ar-457 ranged in a straight line. We start by using DBScan to form clusters of neighboring space-458 points. To avoid clustering spacepoints from multiple particles, we apply several heuristics. 459 The first is that we remove spacepoints within a 3 cm radius of reconstructed keypoints. This 460 length is three times the DBScan maximum distance parameter of 1 cm in order to ensure 461 points from different particles emerging from a vertex or secondary interaction point will not 462 be clustered together. (A cartoon of this step is shown in Figure 6B). This is done to separate 463 spacepoints coming from the locations of neutrino interactions, secondary interactions, or 464 decay. The other heuristic aims to find locations of intersecting trajectories. The approach 465 is to recognize 'vee' patterns using the convex hull around the set of pixels corresponding 466 to the projected spacepoint location on the wire planes. This reuses algorithms built for 467

the one 1-lepton-1-proton exclusive analysis in the previous MicroBooNE low-energy excess search [29]. We use convex hull defect points to identify intersecting trajectories and the location to split the clusters assuming either an 'X'- of 'V'-shaped 3D spatial pattern. (A cartoon of this step is shown in Figure 6C).

We build individual particle tracks by chaining, end-to-end, the straight-line subclusters. 472 We use a recursive depth-first graph traversal algorithm to build chains of subcluster seg-473 ments. This algorithm begins by defining a graph whose nodes are the collection of line 474 segment endpoints. Two types of edges are defined between the nodes. The first edge type 475 (A) connects endpoint nodes belonging to the same subcluster. The second edge type (B) 476 connects endpoint nodes below some max distance. (A cartoon of this step is shown in 477 Figure 6D with the A-type edges represented as solid black line segments and B-type edges 478 as dashed red line segments.) Multiple B-type edges between the endpoints of two line 479 segments can be formed. 480

Once the graph is formed using all the subcluster line segments, a recursive graph traversal 481 algorithm is used to build chains of line segments representing candidate track trajectories. 482 The sub-set of endpoint nodes sufficiently close to designated keypoints serve as starting 483 points. (A cartoon of this step is shown in Figure 6E.) Using depth-first recursion, a tree-484 structured subgraph for each seed node is built by traversing edges of alternating type, 485 starting with A-type edges. Heuristics based on angles and distances between edges and 486 segments were used to choose and prioritize B-type edges to include in the tree. For potential 487 B-type edges less than 3 cm, the cosine between the track segments that this B-edge would 488 connect is required to be greater than zero. For edge lengths between 3 to 10 cm, the cosine 489 between track segments must be greater than 0.7. For lengths longer than 10 cm, the cosine 490 must be greater than 0.9. We allow for such fairly large distances between track segments 491 in order to cross regions of unresponsive wires that occur within the detector. These values 492 were optimized to maximize the completeness of simulated cosmic muon tracks. To prevent 493 loops, nodes can only be visited once. 494

Paths within a tree subgraph that connect the root node to the leaf nodes represent candidate trajectories. Possible paths are selected using the heuristic that true trajectories run along regions of ionization. This is quantified by the fraction of the trajectory length that projects onto locations within the wire plane images that are near pixels with sufficient ionization. Paths satisfying this criterion are scored based on weighted sum of the total path length, the trajectory fraction near ionization, whether the end of the path coincides with
a track-end keypoint, and a measure of the overall trajectory straightness. Valid paths are
then sorted by descending score.

Candidate track particles are created from the set of paths, starting with the highest 503 scoring. The ordered collection of line segments define the trajectory of the track. Track-504 like spacepoints close to the line segments form a cluster associated with the trajectory. Any 505 remaining paths that fork from the current highest-scoring path are used to define secondary 506 tracks that begin at the last common node. Once a track trajectory is created, any segments 507 included in the path are forbidden to be reused. Any remaining path is removed if it includes 508 any A-type edges corresponding to segments included in a track. Track creation continues 509 with the remaining highest-scoring path and completes once the set of valid paths is empty. 510 Candidate tracks are created in this way for all starting nodes. An individual subcluster 511 line segment can be a part of multiple track candidates, as long as the tracks were created 512 using different starting nodes. Once all candidate tracks have been formed for a given pool 513 of track subclusters, refinements to the line segment trajectory are made for each track can-514 didate. The refinements consist of creating new points along the segmented line such that 515 a chosen maximum distance occurs between points. The locations of the expanded set of 516 points are iteratively perturbed using gradient descent in order to minimize squared-distance 517 between projected wireplane positions and pixels with ionization. Once refinements of the 518 line-segment trajectories are completed, 3D spacepoints are associated with each trajectory. 519 First, spacepoints in the sub-clusters used to make the trajectory are added. Second, space-520 points close to keypoints, which were vetoed initially, are added to the trajectory. The 521 collection of spacepoints along with the line segment trajectory represent the candidate par-522 ticle tracks. (The final track candidates in the diagram of Figure 6, defined with both a line 523 segment trajectory and associated spacepoints, are shown in sub-figure F.) 524

# 525 2. Forming shower candidates

The approach taken for forming shower candidates is to assume that shower keypoints are located at the start of a shower and then to collect 3D spacepoints, tagged as shower-like by SSNet, belonging to the shower. Points are added to a candidate shower if they fall within a cylindrical region around the shower's reconstructed direction. To determine the shower



Figure 7: Schematic illustrating steps of the shower reconstruction. (A) Spacepoints with shower-like and in-time labels are collected along with shower keypoints. The shower points are colored orange. Shower keypoints are given random colors. (B) DBscan is used to cluster the points based on neighbor distances. Found clusters are assigned a random color and index. There are some points shown which did not have enough points to form a cluster. (C) The first principal component direction and keypoint define the initial direction of the shower. (D) A subset of points within each cluster near the keypoint is used to define a shower trunk. (E) The trunk direction and keypoint defines a line. Clusters close to this line are added to the shower candidate, defined by a keypoint, shower trunk, and cluster of shower spacepoints.

direction, a shower "trunk" is defined as a line that running along the first 3-10 centimeters of ionization at the start of the shower.

The shower reconstruction begins by gathering, as input, spacepoints that have been filtered to have (1) an SSNet shower score greater than 0.5, (2) a LArMatch 'true' score of 0.8 (the same threshold for accepting spacepoint candidates), and (3) to be associated with pixels that have not been tagged as being out-of-time with the beam, (in other words does not have a cosmic tag). The algorithm also requires a set of shower keypoints. In figure 7a, spacepoints satisfying the conditions are shown as orange circles. Different candidate shower keypoints are also shown in figure 7a in random colors, here blue, red, and magenta.

Next, DBscan is used to build shower subclusters and is run with the following parameters:
a maximum distance of 5.0 cm, minimum cluster size of 20, and max nearest neighbors of
20. The somewhat higher minimum points to form a cluster is meant to reduce the number

of small disconnected shower fragments. In the illustration in figure 7b, three clusters are found are given a random color and index. Note the smaller fragments which do not form a cluster. The first principal component (PC) is then calculated for each cluster. To remove very short clusters, any cluster whose first PC length – measured by the maximum distance between pairs of points projected onto the first PC line – is shorter than 1 cm is rejected. In the illustration in figure 7c, examples of PC axes for each cluster is shown.

Next, the shower keypoints are used to find a good shower "trunk." For all keypoints 548 within 10 cm of the axis-aligned bounding box of each shower cluster, a subset of cluster 549 points within a certain radius of the keypoint are collected. For each subset of points, a 550 first PC axis is found and defines the axis of the shower trunk. A subset of points is made 551 three times for each keypoint and cluster pair, using a radius of 3 cm, 5 cm, and 10 cm. In 552 all cases, the keypoint is required to be at most 1 cm from the nearest cluster spacepoint in 553 order to be able to define a valid shower trunk. In studies of the dE/dx along the true initial 554 direction of simulated electron showers, the energy loss per unit length was most separable 555 between electrons and photons between 1 cm to 3 cm. The upper bound was interpreted 556 to be approximately the length scale where some aspect of the shower's cascade has begun, 557 causing a widely varying dE/dx that differs from just ionization. Of the three candidate 558 trunks, we choose the one to represent the cluster's trunk based on which is the most line-559 like. This is quantified using the ratio between the second-to-first principal component of 560 the cluster's spacepoints. 561

At this point in the shower reconstruction, each shower candidate includes the cluster points, a shower trunk, and the seeding shower keypoint. Figure 7d provides an example where a shower trunk has been found for each of the three clusters in the illustration. Note that a subset of points, marked with a darker color, are tagged as being part of the shower trunk, can fall within different radii of their respective keypoints.

Finally, we attempt to add additional shower points to each candidate shower cluster. We do not add individual points, but instead test to see if we should add an entire cluster's points to a shower candidate. For each shower candidate, we loop through all shower clusters and ask which fraction of the cluster's points are within a volume around the line defined by the shower trunk's direction and the position of the keypoint. The acceptance volume is split into two regions. The first volume is for points in the "forward direction" of the shower, which must be (1) within 5 cm of the trunk axis while (2) it's projected distance

along the axis is less than 50 cm from the keypoint. The second volume is for points in the 574 "backward direction" of the shower. These points must have as projected distance within 575 3 cm of the keypoint and be within 3 cm of the trunk axis. This second volume is meant 576 to help with cases where the shower keypoint is reconstructed a few centimeters into the 577 trunk. If half of the points within the cluster falls within the volume defined by the shower 578 candidate trunk, all of the spacepoints are added to the shower candidate. In our illustrative 579 examples, figure 7e depicts successful tests to add a cluster of points to shower candidates 580 1 and 3 as each have a cluster whose points are within some distance of the trunk's line. 581

Note that the shower cluster merging condition at this point of the reconstruction is rel-582 atively restrictive. We later use the neutrino vertex to help merge shower cluster candidates 583 into bigger, more complete shower clusters. This cluster merging occurs when neutrino in-584 teraction candidates are being constructed. We start the process of building showers by 585 tagging a subset of shower candidates found from the procedure above as "shower prong" 586 candidates. These are intended to represent the beginning of a possibly larger shower emerg-587 ing from a neutrino interaction. Prongs are first identified based on how well they point 588 back to the neutrino vertex. To qualify as a prong, the shortest distance between the line 589 defined by a shower cluster's trunk direction and the neutrino vertex (often described as 590 the impact distance in other scattering contexts) is below 20 cm. The shower prongs that 591 qualify are then sorted by those with the smallest distance to those with the largest. Then, 592 beginning with the prong with the smallest distance, we then loop over all shower clusters 593 and decide on merging each into the prong if a cluster falls within a cone defined by the 594 prong. The cone is defined by an axis whose starting point and direction are defined by the 595 prong's trunk. Because the trunk is a line segment, the endpoint of the trunk closest to the 596 neutrino vertex is designated as the tip of the cone. The trunk line segment is used to define 597 the ray of the cone such that the direction of the ray is away from the neutrino vertex. The 598 opening angle of the prong cone is 30 degrees. This is the angle of a right triangle whose 599 height is approximately 2 Moliere radii (9.04 cm in liquid argon) and whose base is 50 cm 600 (or about 3.5 radiation lengths) [30]. We add other 'test' shower clusters to the prong by 601 determining if the test cluster falls within the prong's cone. To determine this, we ask if the 602 test cluster's trunk endpoint closest to the neutrino vertex is within the 30-degree opening 603 angle. We iteratively define a new prong and associate available shower clusters to it, all the 604 while tagging clusters as unavailable and skipping them if they were used to define a prong 605

or were merged into a prong. In this way, we use the neutrino vertex to help sort the order
of shower candidates and thus bias which ones should serve as the starting prongs on which
to build.

#### 609 F. Interaction Candidate Formation

The formation of neutrino interaction candidates begins with associating neutrino key-610 point candidates with track subcluster segments and shower-trunk candidates. The track 611 subclusters derive from the in-time-track spacepoints. The shower subclusters and trunks are 612 made from the in-time-shower spacepoints. Both types of subclusters are added as 'primary 613 prongs' based on the distance between (1) the vertex and the closest segment endpoint and 614 (2) the neutrino keypoint and the prongs first principal component axis. The graph-based 615 algorithm described above is used to build candidate tracks using only the neutrino keypoint 616 as a seed. The cone-based procedure described above is used to construct shower candidates 617 using the associated shower prongs. For any shower subclusters assigned to multiple shower 618 candidates, we prevent over-counting of visible energy by forbidding subclusters from being 619 added to multiple shower prongs in this context. The track and shower candidates created 620 at this stage of interaction reconstruction are tagged as primary prongs. At this stage, we 621 also correct for potential reconstruction errors due to small clusters of spacepoints being 622 mislabeled as track-like by the SSNet CNN. One algorithm checks for such track-like clus-623 ters that might occur at the beginning of a shower. For each shower prong, a line between 624 its start point and the vertex is defined. We then check for any track clusters with over 90%625 of its spacepoints within 3.5 cm of this line or within 2 cm of the shower's trunk, for which 626 the latter is defined by a line segment up to 10 cm long. We also check for short track-like 627 subclusters that lie deeper within a shower, beyond the trunk. When such track clusters 628 are detected, the track cluster is removed and its spacepoints are added to the shower's 629 spacepoint container. 630

With the set of primary particles defined, the next step of the reconstruction is to add secondary particles to the candidate neutrino interaction. The search for secondaries starts by finding track and shower subclusters whose starting points are within 2 cm of any of the associated primary tracks or whose first principal component forms a line that approaches within 2 cm. For each secondary track prong, the graph-based track builder is used to create track particles. Likewise, for each secondary shower prong, the cone-based shower
building algorithm is used to construct a secondary shower particle. This secondary particle
reconstruction continues to iterate until no additional track-like or shower-like subclusters
are associated with the interaction.

The construction of neutrino candidates concludes with routines to estimate the energy of tracks using range under the assumption of a few particle species. The initial direction of the track is also estimated. Calorimetric estimates of the total ionization are made by summing the pixel values of individual wire plane images. This leads to three plane-specific estimates for each shower. An initial integral-to-energy conversion is applied. Details for these energy estimates are in Section II H.

In addition to neutrino interactions, the reconstruction also builds cosmic muon tracks using the graph algorithm seeded by track-start and track-end keypoints. The tracks are made using clusters coming from the cosmic-track spacepoints.

This interaction-building stage is the final step of the 3D spacepoint-based reconstruction. The neutrino interactions and their candidate primary and secondary particles are saved for analysis. The spacepoints and their associated scores are saved only for those assigned to a particle that is part of a neutrino candidate. These products will be used by the CNN-based particle ID to be described in later sections. The scores of the keypoints are also stored for selection and analysis purposes.

#### 655 G. Reconstruction Validation

The algorithms described in the previous sections are able to efficiently reconstruct neu-656 trino interactions and final state particles. This section presents validation plots exploring 657 vertex and prong reconstruction quality using a sample of MC neutrino interactions (overlaid 658 over cosmic-ray background data) occurring inside the MicroBooNE fiducial volume (defined 659 as 3cm from the edge of the space-charge-corrected TPC boundary as in [17]). The ability 660 of our reconstruction outputs to select CC  $\nu_{\mu}$  and CC  $\nu_{e}$  events with high efficiency and 661 purity is explored in sections III A and III B. These metrics are defined by the fraction of 662 selected events relative to all charged-current events whose vertex occurs within the fiducial 663 volume. 664

#### 665 1. Vertex Validation

Figure 8a shows the efficiency of our neutrino vertex reconstruction as a function of 666 simulated neutrino energy for CC  $\nu_{\mu}$  and CC  $\nu_{e}$  interactions. Vertex efficiency is higher for 667 CC  $\nu_e$  events, but is high in both cases, rising above 80% by 0.5 - 0.6 GeV in neutrino energy 668 and leveling off at around 85% - 90% above 1 GeV. Below 0.5 GeV, vertex reconstruction 669 efficiency drops steeply (as expected), falling below 60% around 0.2 - 0.3 GeV. Figure 8b 670 shows how accurate the vertex reconstruction is in cases where a candidate neutrino vertex 671 is found. From this area normalized distribution of the distance between the reconstructed 672 and true neutrino interaction vertex (for all MC neutrino interactions), we can see that the 673 vast majority of reconstructed vertices are within 1cm of the true position. More specifically, 674 68% of reconstructed vertices are within 9.2mm of the simulated interaction position. The 675 spacing between wires is 3mm, so we can reconstruct vertices within within about three 676 wires, which is quite close to the one-wire-limit on the accuracy of a perfect reconstruction. 677



Figure 8: (a): The fraction of MC  $\nu_{\mu}$ CC and  $\nu_{e}$ CC interactions occurring inside the MicroBooNE fiducial volume in which a neutrino candidate vertex was reconstructed (as a function of simulated neutrino energy). (b): The distance between the true and reconstructed neutrino vertex for all MC neutrino interactions inside the MicroBooNE fiducial volume.

#### 678 2. Prong Validation

To determine the quality of reconstructed prongs, we select a sample of tracks and showers 679 attached to reconstructed neutrino vertices from MC neutrino interactions. Prongs are truth-680 matched to simulated particles from the interaction by projecting all of their spacepoints 681 back into the 2D wire plane images and finding the simulated particle that deposits the 682 most charge in associated 2D pixels. To allow for accurate truth-matching, we require 683 that no more than 20% of the prong's 2D pixel charge come from the overlaid cosmic-ray 684 background data. For each prong, we calculate the reconstruction quality metrics of purity 685 and completeness, where purity is defined as the fraction of the prong's total 2D pixel charge 686 that was produced by the truth-matched simulated particle, and completeness is defined as 687 the fraction of the total 2D pixel charge deposited by the simulated particle that is included 688 in the reconstructed prong. 689

Figure 9 shows plots of purity vs. completeness for prongs that are truth-matched to 690 simulated muons, charged pions, protons, electrons, and photons. The vast majority of 691 reconstructed prongs occupy the high-purity, high-completeness upper-right corner of these 692 plots, indicating a quality reconstruction. However, for protons and, to a greater extent, 693 charged pions, there is a non-trivial population of prongs with high completeness but rela-694 tively low (roughly 40 - 70%) purity. This is largely due to the difficulty in separating out 695 short tracks from the often dense clusters of charge surrounding the immediate vicinity of 696 interaction vertices. Additionally, charged pions often decay, producing (through an inter-697 mediate muon) a small electron shower. In these cases, the electron shower and charged 698 pion track are sometimes reconstructed as part of the same prong, contributing to the popu-699 lation of lower-purity pion prongs. There is also a non-trivial population of electron prongs 700 with high purity, but low completeness. This is caused by either an early, spatially isolated 701 branch of the electron shower getting reconstructed as a separate shower or by the pixels 702 associated with a small stub of the trunk of the electron shower getting tagged as track 703 pixels, causing that stub to get reconstructed as a separate track. However, in these cases, 704 most of the electron shower is almost always reconstructed in a separate prong, and these 705 occasional reconstruction issues can be overcome by identifying such prong fragments by 706 estimating their purity and completeness with the LArPID network (discussed in section 707 III). 708

Muon Prong Purity vs Completeness



(a)

Pion Prong Purity vs Completeness

Proton Prong Purity vs Completeness



Figure 9: Purity vs. completeness for reconstructed prongs (from MC neutrino interactions occurring inside the MicroBooNE fiducial volume) that are attached to neutrino candidate vertices and truth-matched to simulated muons (a), charged pions (b), protons (c), electrons (d), or photons (e).

#### 709 H. Energy Reconstruction

To reconstruct the energy of tracks, we first use the LArPID network discussed in section 710 III to determine the particle type: tracks are classified as either muons, charged pions, 711 or protons based on which of those three LArPID particle scores is highest. Knowing the 712 particle type, we can then use the track length and fits to the kinetic energy vs. range 713 curves of these three particles to determine a kinetic energy for the track. These fits are 714 shown in figure 10 overlaid over a scatter plot of kinetic energy vs. length for simulated 715 muon, charged pion, and proton trajectories (from MicroBooNE MC  $\nu_{\mu}$ CC interactions) 716 that begin and end at least 10cm from the edge of the MicroBooNE active volume. The fit 717 for muons provides accurate results; however, charged pions and protons often interact before 718 ranging out, causing a spread above the fit line for particles in which our range calculation 719 underestimates energy. This range calculation will also of course underestimate the energy 720 of track-like particles that exit the detector. These shortcomings will be addressed in future 721 studies. 722

Shower energy is reconstructed from the visible charge observed in the collection plane,  $Q_{sh}$ , which is linearly related to shower energy. As discussed in more detail in [31], a fit to shower energy vs.  $Q_{sh}$  yields the conversion:

$$E[MeV] = (0.0126 \pm 0.0001)Q_{sh},\tag{4}$$

<sup>726</sup> where the error is from statistical uncertainty in simulated events used in the fit.

Our neutrino energy estimate is then simply calculated as the sum of the reconstructed track and shower energies for all prongs attached to the reconstructed neutrino interaction vertex. This is a measure of visible energy, not a sophisticated neutrino energy reconstruction. A more accurate energy reconstruction that addresses the limitations of the track energy estimate and includes more sophisticated techniques will be introduced in future works.

The accuracy of this visible neutrino energy estimate is illustrated in figure 11, which shows reconstructed vs. true neutrino energy for a sample of MC  $\nu_e$ CC and  $\nu_{\mu}$ CC events. Only simulated interactions in which all neutrino final state particles are contained inside the detector and that were reasonably well reconstructed (a neutrino vertex must have been found with an attached prong that contains at least 60% of the primary lepton's deposited



Figure 10: Kinetic energy vs. range for simulated muons (a), charged pions (b), and protons (c) that begin and end in the detector fiducial volume and were produced in MC  $\nu_{\mu}$ CC interactions. The fits used in track energy reconstruction are shown in blue.

charge) are included in these plots<sup>2</sup>. While the majority of events' reconstructed energy falls
below the overlaid one-to-one line and underestimates the true neutrino energy (as expected
for this visible energy calculation), there is a reasonably strong linear relationship.

# 741 I. LArPID: A Prong Classification CNN

To aid in event selections and physics analyses, another CNN, the Liquid Argon Particle **ID**entification (LArPID) network, was developed to provide additional information about reconstructed prongs. CNNs have effectively been used for particle identification in the past (e.g. in NOvA [32]) and hold particular promise for LArTPCs given their ability to

<sup>&</sup>lt;sup>2</sup> Of simulated contained  $\nu_e$ CC events with a reconstructed vertex, 66% have an attached shower containing at least 60% of the simulated electron's deposited charge. For  $\nu_{\mu}$ CC events (same conditions), 74% have an attached track with at least 60% of the simulated muon's deposited charge.



Figure 11: Reconstructed vs. true neutrino energies for MC  $\nu_e$ CC (a) and  $\nu_{\mu}$ CC (b) interactions that were successfully reconstructed (a prong from a neutrino candidate vertex was reconstructed with at least 60% of the simulated primary lepton's deposited charge) and in which all simulated neutrino final state particles are contained (begin and end inside the detector).

<sup>746</sup> image neutrino interactions with mm-scale precision. While the primary aim of LArPID is
<sup>747</sup> to perform particle identification, it also predicts the input prong's production process and
<sup>748</sup> useful reconstruction quality metrics. Specifically, for each input prong, LArPID predicts:

- Particle type: The network outputs five scores indicating how likely it is that the prong was produced by a muon, electron, photon, charged pion, or proton. As the vast majority of charged particles produced in MicroBooNE neutrino interactions are of one of these types, other very rare particles (e.g. kaon, lambda, or sigma particles) are ignored. While the prong is assigned the particle type with the highest score, as we will see in section III A, taking into account all five particle scores is useful in quantifying how confident we can be with this classification.
- Production process: The network outputs three scores indicating how likely it is that the prong represents a primary final state particle produced in the neutrino interaction, a secondary particle with a charged parent, or a secondary particle with a neutral parent. Rather than attempt to classify all common secondary particle production processes (Michel decays, delta ray production, pion decay, etc.) these broad classes were chosen to simplify the prediction while accomplishing its primary aim: distinguishing primary final state particles from secondaries. The two most general

types of observable secondary topology classes - those where the secondary prong does
(charged parent) and does not (neutral parent) originate at the end point of another
cluster - were chosen to provide additional information about secondaries and aid the
network in organizing prongs into general topology classes. This production process
prediction provides another valuable tool to aid in interpreting events.

- Purity: The fraction of visible energy in the prong that was deposited by the true particle. Here, visible energy is calculated as the sum of all pixel values for all 2D wire-plane-image pixels used in the 3D space points that make up the reconstructed prong. As discussed in section III3, when training the network on Monte Carlo simulation, the labelled truth particle is the simulated particle that deposits the most visible energy in the input reconstructed prong.
- Completeness: The fraction of all visible energy deposited by the true particle that was reconstructed in the input prong (where visible energy and "true particle" are defined as above for the purity prediction).

Analyzing these network outputs for all reconstructed prongs attached to a candidate 777 neutrino interaction vertex provides valuable information about both the prongs and the 778 candidate neutrino interaction. The particle classification outputs not only aid in identi-779 fying particles and selecting neutrino interactions with desired final states, but could also 780 allow for a more accurate neutrino energy estimate by providing a robust particle hypothesis 781 in e.g. range-based momentum calculations or neural-network based energy estimation tech-782 niques utilizing high-level reconstruction outputs. In addition to organizing particles into 783 parent/daughter hierarchies for true neutrino interactions, the particle production process 784 can be used to veto mis-reconstructed neutrino interaction vertices placed at the position 785 of e.g. a particle decay. As shown in section III A, it is particularly helpful in CC  $\nu_e$  event 786 selections as it can veto background events where the candidate primary electron prong is 787 in fact a secondary (for example a charged pion decay product or cosmic Michel electron). 788 And the completeness and purity metrics allow for the identification of poorly reconstructed 789 prongs: prongs reconstructed from energy depositions of a variety of different particles or 790 those representing a fragment of a true particle. These reconstruction quality metrics can be 791 used to better understand reconstructed neutrino interactions and, in the future, to improve 792
the reconstruction as inputs to downstream algorithms or networks that could reorganize
clusters into prongs that better represent particle trajectories.

The following sections detail this LArPID network's inputs (section III1), architecture (section III2), training details (section III3), and performance (section III4). Preliminary studies on interpreting the model are discussed in section III5.

# <sup>798</sup> 1. Network Inputs and Image Preprocessing

The LArPID network operates on all three 2D wire-plane images (with tagged cosmic 799 pixels removed) of both the input reconstructed prong and the full event. Going back 800 to the 2D images provides the network with information that may have been lost during 801 reconstruction as a result of dead channels or other errors. For example, in the probable CC 802  $\nu_e$  data event shown in figure 12, shower pixels near the interaction vertex are present in the 803 collection plane, but are missing in both the U and V planes. As a result, no 3D space points 804 could be formed near the vertex, and the reconstructed 3D shower prong begins at a distance 805 from the reconstructed neutrino interaction vertex. If considering only the 3D reconstruction 806 outputs, this might indicate that the shower is a photon (which travel a distance from the 807 vertex before pair-converting and depositing energy). However, by operating on the original 808 2D wire-plane inputs, the LArPID network can see the shower extending back to the vertex 809 in the collection plane and classifies this shower as an electron. 810

Including the full-event context images, with all non-cosmic-tagged pixels, provides the 811 network with a wealth of additional information that aids in all the network's tasks. Seeing 812 the full event improves particle identification accuracy by allowing the network to learn 813 physical features associated with different particle types. For example, photons start at a 814 distance from the interaction vertex, whereas electrons begin depositing energy directly at 815 the vertex. Neutral pions decay into a pair of photons, so the network can learn that when 816 it sees two showers pointing back to the vertex these are likely photons. Preliminary studies 817 indicating that the network indeed picks up on this kind of context information in assigning 818 particles scores are presented in section III5. The context information is of course also 819 needed to observe parent or fellow neutrino final state particles in distinguishing between 820 primaries and secondaries in the production process classifier. Finally, allowing the network 821 to observe when prong pixels are embedded in a larger cluster or a mix of different clusters 822



Figure 12: Bottom: zoomed in view of three wire plane images for a probable CC  $\nu_e$  interaction in a MicroBooNE open dataset. The views are from the U induction plane (left), the V induction plane (center), and the Y collection plane (right). Top: Reconstructed neutrino candidate for the same event with PMT positions recording flashes highlighted (purple: reconstructed neutrino vertex position, copper: 3D space points in reconstructed shower, green: 3D space points in reconstructed track). This event passed our selection even though there is a visible gap in 3D spacepoints between the shower and vertex caused by unresponsive wires in the U and V planes. However, the prong-CNN still designated the shower electron-like likely due to the shower visibly starting from the vertex in the Y plane. This is a candidate example where using the low-level 2D information has helped overcome downstream reconstruction errors.

<sup>823</sup> is needed for accurate completeness and purity estimates.

The prong and context images passed to the network are processed as follows. To obtain the prong images, 3D space points in the reconstructed prong are projected back into the 2D wire-plane images to obtain all associated pixels. To reduce computational requirements, these images are then cropped to a 512x512 pixel (153.6 x 153.6 cm) window. This window size is large enough to encompass most charged particles from neutrino interactions in Micro-BooNE. This crop is performed separately in each wire plane. In a given wire-plane image, when the full set of prong pixels does fit within this window, the crop is centered around

the middle of the prong (the point half-way between the min and max row and column). 831 If the prong pixels do not fit within this window, the crop is centered around the end of 832 the prong for tracks and around the beginning of the prong for showers. This decision was 833 taken as most of the information in distinguishing muon, charged pion, and proton tracks 834 lies at their end (as the particle slows down and potentially decays), whereas the informa-835 tion needed to distinguish between photon and electron showers lies at the beginning, in 836 the shower trunk. In each wire-plane, the context image is cropped around the same region 837 as the prong image. Before passing these six images (one prong and one context image for 838 all three wire-planes) to the network, pixel values are normalized into the range of roughly 839 -1 to 1 by subtracting the mean and dividing by the standard deviation of all final state 840 particle pixels in a large set of simulated neutrino interactions. An example of the six input 841 images passed to the network for a reconstructed charged pion track from a simulated CC 842  $\nu_{\mu}$  interaction is provided in figure 13. 843

## 844 2. Network Architecture

The LArPID network architecture is illustrated in figure 14. A 34-layer residual network 845 (ResNet34) [24] was chosen for the CNN<sup>3</sup>. LArPID's ResNet34 CNN has two input channels 846 for the prong and context image of one wire plane, and it operates separately on each 847 wire plane using shared weights for all three. A 2D adaptive average pooling operation 848 is performed on the output of the final layer, providing 512 learned features for each of 849 the three wire planes. These features are concatenated into a single 1536-length feature 850 vector summarizing information learned about the input prong. This concatenated feature 851 vector is then used as input to four multi-layer perceptrons (MLPs) used to perform the 852 four network tasks. Each MLP has a single hidden layer<sup>4</sup>. The particle classification MLP 853 has a five-neuron output layer, whose logits are passed through a softmax to provide the 854 muon, charged pion, proton, electron and photon scores. The particle production process 855 classification MLP uses a length three output layer and softmax to provide the primary, 856 secondary with charged parent, and secondary with neutral parent scores. The purity and 857

<sup>&</sup>lt;sup>3</sup> While slightly improved performance might be achieved by using an deeper network, this would have increased the computational complexity and made the network difficult to deploy on cpus as required for large-scale MicroBooNE data processing. An 18 layer ResNet CNN was tested as well, but was found to provide lower performance.

<sup>&</sup>lt;sup>4</sup> Increasing the number of hidden layers was found to increase the time it took the model to converge during training without improving performance



Figure 13: Example LArPID input images for a reconstructed charged pion track from a simulated CC  $\nu_{\mu}$  interaction. Top row: prong images for all three wire planes. Bottom row: full event context images for all three wire planes

completeness regression MLPs use a single-neuron output layer and sigmoid to provide purity
 and completeness predictions in the required physical range of 0 to 1.

# 860 3. Training

The LArPID network was trained on a sample of over 652,000 reconstructed prongs from MicroBooNE neutrino Monte Carlo simulations overlaid over off-beam cosmic-ray background data [MC citation]. Only prongs attached to reconstructed candidate neutrino interaction vertices were considered. If an event had multiple reconstructed neutrino vertices, only prongs attached to the vertex with the highest LArMatch neutrino keypoint score were selected for training. Two additional requirements were imposed on prongs selected for the training sample:



Figure 14: LArPID network architecture with the example inputs from figure 13.

• Training prongs must have at least 10 above-noise-threshold pixels (which span 3cm in the detector) in all three wire-plane images. Studies were performed to test if increasing this minimum-pixel threshold might improve performance on larger prongs that are primarily considered in neutrino event selections. However, it was found that the network, when trained only on larger (minimum pixel threshold = 90) prongs, did not perform better on a validation set including only such large prongs than when trained on a prong sample including the smallest reconstructed prongs.

• To allow assignment of truth labels, no more than 20% of charge included in training prongs could come from cosmic-ray contamination.

To assign truth labels for training and validation, 3D space points included in reconstructed prongs are projected back into the three wire-plane images to obtain all associated 2D pixels. The total amount of charge in all prong pixels that was deposited by each simulated charged particle produced in the neutrino interaction is summed, and the trueparticle-type label is assigned as the simulated particle that deposited the most charge. The total charge deposited in the entire detector by this truth-matched simulated particle is also calculated, and the true completeness value is assigned as the fraction of this charge included in the reconstructed prong. The purity value is assigned as the fraction of all charge in the reconstructed prong that is contributed by this truth-matched simulated particle. Finally, the particle production process label is assigned according to how the truth-matched simulated particle was generated. The number of prongs in the training sample truth-matched to each of the five particle types is shown in table I below.

muons	charged pions	protons	electrons	photons
$163,\!987$	53,871	$266,\!653$	90,940	76,915

Table I: Number of prongs truth-matched to each of the five particle classes in the LArPID training sample

The network was trained over this sample for 20 epochs using a multi-task loss function 889 with learned weights following the procedure outlined in [33]. A loss must be defined for 890 each of LArPID's four tasks (predictions) and combined to form the network's full loss 891 function. The relative weight attached to each task-specific loss function can significantly 892 impact the network's performance, so the value chosen for these weights is important. The 893 method employed in [33] treats task weights as learned network parameters that can be 894 optimized during training. The authors found that this technique can provide superior 895 performance than even optimal hard-coded weights (e.g. hard-coded values of  $w_1$  and  $w_2$  in 896 the two-task loss function  $\mathcal{L} = w_1 \mathcal{L}_1 + w_2 \mathcal{L}_2$ ). We confirmed this in the case of LArPID by 897 varying hard-coded task weights used in combining task specific loss functions. We found 898 that the network trained with learned weights outperformed the network trained with any 899 set of hard-coded weight values. We further found that the network's particle classification 900 performance, perhaps the most important network task, was no better when trained only on 901 that task than when trained on all four tasks using learned task weights. Therefore, using 902 the technique outlined in [33], the loss function used to train LArPID was defined as: 903

$$\mathcal{L} = e^{-s_{cr}} \mathcal{L}_{MSE}(\hat{y}_{cr}, y_{cr}) + e^{-s_{pr}} \mathcal{L}_{MSE}(\hat{y}_{pr}, y_{pr}) + 2e^{-s_{ic}} \mathcal{L}_{CE}(\hat{y}_{ic}, y_{ic}, w_{ic}) + 2e^{-s_{pc}} \mathcal{L}_{CE}(\hat{y}_{pc}, y_{pc}, w_{pc}) + s_{cr} + s_{pr} + s_{ic} + s_{pc}$$
(5)

where  $\mathcal{L}_{MSE}$  and  $\mathcal{L}_{CE}$  are the mean squared error (for regression tasks) and cross entropy

(for classification tasks) loss functions, respectively; y and  $\hat{y}$  are the true and predicted 905 network outputs, respectively, for a given input and network task; the s parameters are 906 the learned task-specific loss weights; the subscripts cr, pr, ic, and pc denote quantities 907 for the completeness regression, purity regression, particle-identification classification, and 908 particle-production-process classification tasks, respectively; and  $w_{ic}$  and  $w_{pc}$  are vectors of 909 class weights based on the number of prongs belonging to each particle identification and 910 production process classes, respectively, in the full training sample. These class weights are 911 calculated once upfront and used to weight contributions to the cross entropy loss functions 912 to account for class imbalances. This ensures, for example, that the network doesn't learn 913 to increase the probability of classifying all inputs as protons simply because there are more 914 proton-labelled prongs in the training sample than any other type of particle. 915

Additional training details are as follows:

• One data augmentation technique was employed to reduce over-fitting: input images 917 were randomly flipped horizontally or vertically, each with a probability of 50%. As 918 demonstrated in figure 15, which shows overall particle classification accuracy for the 919 training sample and an independent validation sample with 50,000 prongs (10,000 per 920 particle type), over-fitting was not a significant issue. Similar few percent differences 921 were observed in the training vs. validation performance of the other network tasks. 922 More details and discussion on network performance in the validation sample are 923 presented in section III4. 924

925

• The AdamW gradient descent algorithm [34] was used to update network weights.

• The single-cycle cosine annealing learning rate scheduler shown in figure 16 was used. 926 This type of variable learning rate has been found to reduce the number of training 927 epochs required for convergence [35]. The minimum and maximum learning rate values 928 used in the scheduler were chosen by varying the learning rate in a test training run 929 and determining the range of rate values over which the model continues to converge. 930 A variety of other single-cycle, oscillatory, and stepped learning rate schedulers were 931 tested, but none achieved better performance or faster convergence than the chosen 932 schedule depicted in figure 16. 933



Figure 15: Overall particle classification accuracy for the training sample and an independent validation sample with 50,000 prongs (10,000 per particle type) as a function of training iteration.



Figure 16: The learning rate scheduler used to train the LArPID network, shown as a function of training iterations. The full schedule lasts for 20 epochs.

# 934 4. Network Performance

The performance of the LArPID network was tested on an independent validation sample of 50,000 reconstructed prongs (10,000 of each particle type: muons, charged pions, protons, electrons and photons). The same selection criteria detailed in section III1 used to construct the training sample were used for this validation sample. For the classification task results, an additional requirement that at least 60% of the validation prongs' total pixel charge be contributed by a single simulated particle (true prong purity > 60%) was imposed. This requirement was placed to ensure sensible truth labels could be assigned.<sup>5</sup>

<sup>942</sup> The network achieved an impressive overall validation accuracy of 91.8% on the particle

<sup>&</sup>lt;sup>5</sup> A version of the network was also trained with the same true prong purity > 60% requirement, but it was found that this did not improve the network's classification performance on a purity > 60% validation sample. This requirement was therefore not ultimately imposed on the training sample so that the network could be trained to make more accurate purity and completeness predictions in cases where purity < 60%.

<sup>943</sup> identification task. A confusion matrix showing the accuracy for each particle type is shown
<sup>944</sup> in table II. The per-particle validation accuracy is very high for all five particle types, and
<sup>945</sup> when the network does mis-classify a prong, it almost always applies the label of a particle
<sup>946</sup> that leaves similar signatures in the detector. For example, mis-classified electrons are almost
<sup>947</sup> always assigned a photon label (and vice versa) and mis-classified charged pions are almost
<sup>948</sup> always assinged a muon label (and vice versa).

	True $e^{\pm}$	True $\gamma$	True $\mu^{\pm}$	True $\pi^{\pm}$	True p
Fraction classified as $e^{\pm}$	84.5%	5.2%	0.1%	0.5%	0%
Fraction classified as $\gamma$	12.7%	94.3%	0.2%	0.2%	0.1%
Fraction classified as $\mu^{\pm}$	0.4%	0.1%	93.9%	11.5%	0.3%
Fraction classified as $\pi^{\pm}$	2.3%	0.3%	5.6%	86.5%	1.6%
Fraction classified as $p$	0.1%	0.1%	0.2%	1.4%	97.9%

Table II: A confusion matrix showing LArPID's particle classification accuracy in the validation sample: the fraction of prongs truth matched to each particle type that LArPID classified as an electron  $(e^{\pm})$ , photon  $(\gamma)$ , muon  $(\mu^{\pm})$ , charged pion  $(\pi^{\pm})$ , or proton (p) (columns sum to 100%).

The network's overall validation accuracy on the particle-production-process classification task was similarly high, at 89.0%. As shown in table III, accuracy is high for all three production-process classes. Accuracy is highest for identifying secondaries with a neutral parent, likely as this signature (a prong created with no other tracks or showers originating at it's start position) is more unique than the other two classes.

	True primary	True neutral parent	True charged parent
Fraction classified as primary	87.8%	3.4%	6.5%
Fraction classified as neutral parent	2.9%	93.6%	6.9%
Fraction classified as charged parent	9.3%	3.0%	86.7%

Table III: A confusion matrix showing LArPID's particle-production-process classification accuracy in the validation sample: the fraction of prongs with each true production-process class that LArPID classified as a primary neutrino-final-state particle, a secondary with a charged parent, or a secondary with a neutral parent (columns sum to 100%).

The validation accuracy of the network's completeness and purity predictions are illustrated in figure 17, which shows 2D histograms of the predicted vs. true reconstruction quality metrics. For a given range of true completeness or purity values, there is a nontrivial spread in the predicted values. However, the bulk of the prongs in these heat maps



Figure 17: A 2D histogram showing predicted vs. true completeness (a) and purity (b) for prongs in the validation sample.

do roughly follow a one-to-one line. So while the exact value of LArPID's completeness or purity prediction for a given prong should not be interpreted with extremely high confidence, these predictions are robust in revealing whether the input prong is likely to be a small fragment of a true particle, a mostly complete reconstruction, or something in between (completeness) and, similarly, whether it is likely to be reconstructed from a mix of different particles or mostly from a single particle (purity).

## 964 5. Interpreting the Model

Preliminary image manipulation studies were carried out to shed light on what informa-965 tion LArPID is using from input images to make its predictions. While clear decision-making 966 algorithms cannot be extracted from the complex network of neurons in deep learning mod-967 els, these interpretability studies can provide valuable insights into how neural networks are 968 making decisions. The technique employed here involves testing hypotheses on what infor-960 mation is being used in the network by providing the model with a set of counter-factual 970 images. This is done by replacing an input reconstructed prong or a particle from the context 971 image with another simulated particle and seeing how the network output changes. 972

An example of one such image manipulation study is shown in figure 18. Here, we checked to see if the network is learning, from examples of  $\pi^0$  decay photons, that when two electromagnetic showers' initial trajectories can be traced back to an intersection (the  $\pi^0$ decay position) near the interaction vertex, that these showers are likely photons. Figure



Figure 18: One wire-plane prong image (a) and context image (b) for a reconstructed photon prong produced during a  $\pi^0$  decay in a simulated CC  $\nu_{\mu}$  interaction. A modified context image (c) in which the input photon prong's companion  $\pi^0$  decay photon is removed. With the original inputs (a and b), LArPID outputs an electron score of 0.027 and photon score of 0.97. With the modified inputs (a and c), LArPID outputs an electron score of 0.21 and photon score of 0.77.

18 (a) and (b) show (for one wire-plane) the prong and context images for a reconstructed 977 photon shower produced during a  $\pi^0$  decay. The second  $\pi^0$  decay photon is clearly visible in 978 the context image. With these inputs, the network confidently and correctly predicted that 979 the input prong is a photon, with photon and electron scores of 0.97 and 0.027, respectively. 980 The network was then presented with the same input prong images but modified context 981 images (figure 18c) that had the second  $\pi^0$  decay photon removed. With these inputs, 982 the network's confidence in its photon prediction decreased significantly, with photon and 983 electron scores of 0.77 and 0.21, respectively. The same context manipulation had a similar 984 effect in other examples of input photon prongs from  $\pi^0$  decays, indicating that the network 985 has indeed, as expected, learned to increase its photon scores for input showers that are 986 consistent with  $\pi^0$  decays. 987

Another set of image manipulations for an example LArPID input is shown in figure 19. Panels (a) and (b) show (for one wire-plane) input images for a prong (from a simulated CC  $\nu_{\mu}$  interaction) that is reconstructed from both a short charged pion track and the electron shower produced following the pion decay. As the majority of this reconstructed prong comes from the simulated electron, the network predicts that this prong is an electron, with electron and charged pion scores of 1 and  $2.4 \cdot 10^{-3}$ , respectively.

<sup>994</sup> We wanted to test how the network's individual particle scores are impacted when an



Figure 19: One wire-plane prong image (a) and context image (b) for a prong reconstructed from a charged pion and an electron produced during the pion decay in a simulated CC  $\nu_{\mu}$ interaction. A modified prong (c) and context image (d) in which the charged pion and its decay electron were replaced by a simulated electron with the same start position and momentum and the original charged pion. A second set of modified prong (e) and context (f) images in which the same substitution was performed with another simulated electron, but the replacement electron was simulated to begin at a short distance from the neutrino interaction position. LArPID's output electron, photon, and charged pion scores were 1,  $8.9 \cdot 10^{-4}$ , and  $2.4 \cdot 10^{-3}$ , respectively, for the original images (a and b); 0.99,  $6.5 \cdot 10^{-3}$ , and  $1.8 \cdot 10^{-4}$ , respectively, for the first set of modified images (c and d); and  $3.8 \cdot 10^{-4}$ , 1, and  $2.7 \cdot 10^{-6}$ , respectively, for the second set of modified images (e and f).

input prong is reconstructed with significant contributions from different particles. In cases 995 such as these, can information about what combination of particles contribute to a low-purity 996 prong be gleaned from the individual particle scores? In figure 19 (c) and (d), the input prong 997 was replaced with a pure simulated electron with the same start position and momentum 998 as the original charged pion. With these inputs, the network's pion score decreased to 999  $1.8 \cdot 10^{-4}$ . A similar set of manipulations on combined charged pion-electron prongs yielded 1000 similar results, indicating that the charged pion score for classified electron prongs can be 1001 used to determine if such prongs likely came from a charged pion decay. This feature is 1002

exploited in the CC  $\nu_e$  selection of section III A to reduce CC  $\nu_{\mu}$  backgrounds.

An additional set of image manipulations shown in figure 19 verify that the network is 1004 using the context images to learn that showers that start at a distance from an interaction 1005 vertex are more likely to be photons, and those that start at the vertex are more likely to 1006 be electrons. In panels (e) and (f), a similar manipulation is performed in which the input 1007 prong was replaced with a simulated electron, but this time with a start position at a small 1008 distance from the interaction vertex. With these inputs, even though the input is a true 1000 electron, the network confidently classifies it as a photon prong, with photon and electron 1010 scores of 1 and  $3.8 \cdot 10^{-4}$ , respectively. A similar set of manipulations in which simulated 1011 electrons were placed at a distance from an interaction vertex yielded the same result (a 1012 confident photon prediction), indicating that the network has indeed learned to use this 1013 context information for electron/photon discrimination. 1014

These tests demonstrate the utility of such image manipulation studies in learning how the network is making decisions. In a future work, these manipulations will be performed at scale and the results quantified for a more complete set of counter factuals. This will improve understanding of the model, increase confidence in its predictions, and inform how its outputs might more effectively be used in event selections and physics analyses.

# 1020 III. DEMONSTRATION: SELECTION OF INCLUSIVE $\nu_e CC$ AND $\nu_{\mu} CC$ INTER-1021 ACTIONS IN MICROBOONE

## 1022 A. CC nue inclusive selection cuts

As a demonstration of the effectiveness of these reconstruction tools, we have developed 1023 a set of inclusive CC  $\nu_e$  selection criteria utilizing the output of the LArMatch and LArPID 1024 networks. As we will show, an effective, high purity and efficiency CC  $\nu_e$  selection can 1025 be achieved by selecting LArMatch-identified neutrino candidate vertices and filtering out 1026 cosmic and neutrino backgrounds with the Wire-Cell based cosmic tagger discussed in section 1027 II A and cuts on LAPID outputs of attached prongs. For this study, we use off-beam data 1028 to analyze the cosmic-ray background and simulated neutrino interactions overlaid over 1029 cosmic-ray background data for CC  $\nu_e$  and neutrino background events. 1030

The full set of CC  $\nu_e$  selection criteria is provided in table IV. We will examine the impact

<sup>1032</sup> of adding each selection cut one at a time. With each new cut, we will then discuss the <sup>1033</sup> motivation for its inclusion, show distributions of the cut variable for signal and background, <sup>1034</sup> show data/MC comparisons of reconstructed neutrino energy for events passing the new <sup>1035</sup> selection criteria using a small 4.4·10<sup>19</sup> POT MicroBooNE open data sample, and show the <sup>1036</sup> MC-predicted impact of the new cut on efficiency as a function of true (simulated) neutrino <sup>1037</sup> energy. A new "cut set" is defined in table IV as a set of selection criteria including a newly <sup>1038</sup> specified cut along with all previous cuts.

Table IV: Inclusive CC  $\nu_e$  Selection Cuts

Cut	Notes
LArMatch-identified neutrino candidate vertex found in-	Added in cut set 1 (included
side the fiducial volume	in cut sets 1-6 and final set)
3D space points of prongs attached to neutrino candidate	Added in cut set 2 (included
do not all overlap with Wire-Cell-tagged cosmics	in cut sets 2-6 and final set)
No LArPID-identified muon tracks are attached to neu-	Added in cut set 3 (included
trino candidate	in cut sets 3-6 and final set)
At least one LArPID-identified electron shower attached to neutrino candidate	Added in cut set 4 (included in cut sets 4-6 and final set)
The largest identified electron was classified by LArPID	Added in cut set 5 (included
as a neutrino final state particle	in cut sets 5-6 and final set)
No tracks attached to neutrino candidate have a high LArPID muon score: max $\log(\text{muon score}) < -3.7$	Added in cut set 6 (included in cut set 6 and final set)
The largest identified electron was classfied by LArPID as an electron with high confidence: log(electron score) $- (\log(\text{pion score}) + \log(\text{photon score}))/2 > 7.1$	Added in final cut set

The first CC  $\nu_e$  selection criteria is that a LArMatch-identified neutrino interaction vertex 1039 was found inside the detector fiducial volume. For our neutrino selections, we define the 1040 fiducial volume as 3cm from the space-charge corrected TPC boundary as in [17]. Data 1041 and MC reconstructed neutrino energy distributions with only this requirement are shown 1042 in figure 20a. The data excess seen here and as additional cuts are applied is not unique 1043 to our CNN-based reconstruction and selection and has been seen in other frameworks. As 1044 we will show in section IIID, data and predictions with the full set of selection cuts are 1045 consistent once accounting for statistical and systematic uncertainties. The MC-predicted 1046 CC  $\nu_e$  selection efficiency with just this vertex reconstruction requirement is shown in figure 1047 20b. Vertex finding has a non-trivial impact on efficiency at low (<500 MeV) neutrino 1048 energies where electron showers and other prongs are small and more difficult for LArMatch 1049



Figure 20: (a): Data/MC reconstructed neutrino energy comparison of events selected by CC  $\nu_e$  cut set 1 with  $4.4 \cdot 10^{19}$  POT of MicroBooNE run1 data. (b): MC-predicted CC  $\nu_e$  efficiency vs. true neutrino energy with CC  $\nu_e$  cut set 1. The CC  $\nu_e$  cut set 1 only contains the requirement that a LArMatch-identified neutrino vertex was reconstructed inside the fiducial volume. Cut sets are defined in table IV.

## <sup>1050</sup> to identify and separate from cosmic background.

<sup>1051</sup> If LArMatch identifies more than one neutrino keypoint cluster in an event, we select the <sup>1052</sup> one with the highest keypoint score as the candidate neutrino interaction vertex. Further <sup>1053</sup> selection criteria apply to prongs attached to this candidate interaction vertex.

There is still a significant cosmic-ray background after selecting events with LArMatch-1054 identified neutrino candidates. The majority of this background can be removed with the 1055 Wire-Cell cosmic tagger discussed in section IIA. Figure 21a shows neutrino and cosmic 1056 background distributions for the fraction of 3D points in any cluster attached to the neutrino 1057 candidate vertex that was tagged as cosmic. Events in the final cosmic-dominated bin with 1058 100% cosmic overlap (events where all hits in all prongs attached to the vertex have at least 1059 one constituent pixel that was tagged as cosmic by the Wire-Cell cosmic tagger) are rejected. 1060 Figure 21b shows the new reconstructed neutrino energy distributions with this requirement 1061 included (with "cut set 2"). Figure 21c compares the efficiency curve for this "cut set 2" 1062 to "cut set 1," which only includes the neutrino vertex reconstruction requirement. This 1063 cosmic-ray rejection cut does not have a large impact on CC  $\nu_e$  efficiency. 1064

Further cuts on the LArPID outputs of prongs attached to the candidate neutrino vertex can remove almost all of the remaining cosmic and neutrino backgorund. As a first step, to remove most of the CC  $\nu_{\mu}$  background and some of the remaining cosmic background,



Figure 21: (a): MC and off-beam cosmic background data distributions of the fraction of hits associated with the candidate neutrino vertex that were constructed from pixels tagged as cosmics. Events in the final bin were rejected as the new requirement in CC  $\nu_e$ cut set 2. (b): Data/MC reconstructed neutrino energy comparison of events selected by CC  $\nu_e$  cut set 2 with 4.4·10<sup>19</sup> POT of MicroBooNE run1 data. (c): MC-predicted CC  $\nu_e$ efficiency vs. true neutrino energy with CC  $\nu_e$  cut sets 1 and 2, and the ratio of these two efficiency curves. Cut sets are defined in table IV.

events with identified muons are rejected. Figure 22a compares signal and background distributions for the number of reconstructed muons - the number of LArPID identified muon tracks attached to the candidate neutrino vertex - in events remaining after applying "cut set 2." The requirement that no reconstructed muons are present in the event was added in "cut set 3." Figure 22 (a) and (b) show the reconstructed neutrino energy distributions and efficiency curve comparisons for cut sets 2 and 3. This muon-track rejection cut does not have a large impact on efficiency.

<sup>1075</sup> Now that events with identified muons have been removed, we select events with identified



Figure 22: (a): MC and off-beam cosmic background data distributions of the number of LArPID-identified muon tracks (reco muons) attached to the candidate neutrino vertex. The requirement that no reco muons are present was added in CC  $\nu_e$  cut set 3. (b): Data/MC reconstructed neutrino energy comparison of events selected by CC  $\nu_e$  cut set 3 with  $4.4 \cdot 10^{19}$  POT of MicroBooNE run1 data. (c): MC-predicted CC  $\nu_e$  efficiency vs. true neutrino energy with CC  $\nu_e$  cut sets 2 and 3, and the ratio of these two efficiency curves. Cut sets are defined in table IV.

electrons. Figure 23a shows the distribution of the number of LArPID-identified electron showers for remaining signal and background events. The requirement that at least one electron shower was identified was added in "cut set 4." This removes the majority of the remaining neutrino and cosmic backgrounds, but has a moderate impact on our CC  $\nu_e$ selection efficiency across neutrino energies (see figure 23c). The data/MC reconstructed neutrino energy comparison with "cut set 4" is shown in figure 23b.

<sup>1082</sup> As can be seen in figure 23a, it is not rare in true CC  $\nu_e$  events for multiple electron showers <sup>1083</sup> to be identified. This is generally not due to LArPID incorrectly classifying showers, but



Figure 23: (a): MC and off-beam cosmic background data distributions of the number of LArPID-identified electron showers (reco electrons) attached to the candidate neutrino vertex. The requirement that at least one reco electron is present was added in CC  $\nu_e$  cut set 4. (b): Data/MC reconstructed neutrino energy comparison of events selected by CC  $\nu_e$  cut set 4 with 4.4·10<sup>19</sup> POT of MicroBooNE run1 data. (c): MC-predicted CC  $\nu_e$  efficiency vs. true neutrino energy with CC  $\nu_e$  cut sets 3 and 4, and the ratio of these two efficiency curves. Cut sets are defined in table IV.

clustering errors in which small fragments of the true primary electron are reconstructed as a different shower. In these cases, one reconstructed shower tends to carry the majority of the true electron's deposited charge. The candidate primary electron is therefore identified as the LArMatch-identified electron shower with the most charge.

The majority of the remaining cosmic and neutrino background can be removed by placing additional cuts on the LArPID outputs for this candidate primary electron shower. In much of the remaining background, a true electron is in fact present, but as a secondary, e.g. a Michel electron, delta ray, or an electron produced after a charged pion decay. Figure 24a

Production Process Class for Largest Electron Showe



Figure 24: (a): MC and off-beam cosmic background data distributions of the candidate primary electron shower's LArPID production process class output. The requirement that the candidate primary electron was classified by LArPID as a primary particle was added in CC  $\nu_e$  cut set 5. (b): Data/MC reconstructed neutrino energy comparison of events selected by CC  $\nu_e$  cut set 5 with  $4.4 \cdot 10^{19}$  POT of MicroBooNE run1 data. (c): MC-predicted CC  $\nu_e$  efficiency vs. true neutrino energy with CC  $\nu_e$  cut sets 4 and 5, and the ratio of these two efficiency curves. Cut sets are defined in table IV.

shows the output of the LArPID particle production classifier for the candidate primary 1092 electron in signal and background events remaining after "cut set 4." This classifier is able 1093 to accurately separate out the true primary electron showers from the candidates produced 1094 in background events, almost all of which are classified as secondaries. The requirement that 1095 the primary electron candidate was classified by LArPID as a neutrino final state particle 1096 was therefore added in "cut set 5." This new requirement has a fairly small impact on CC  $\nu_e$ 1097 selection efficiency except at very low (<200 MeV) neutrino energies (see figure 24c). The 1098 new reconstructed neutrino energy distributions are shown in figure 24b. 1099



Figure 25: (a): MC and off-beam cosmic background data distributions of the log of the highest LArPID muon score for any track attached to the candidate neutrino vertex. The bin at -20 contains events with no tracks. The requirement that no track have a log(muon score) above -3.7 was added in CC  $\nu_e$  cut set 6. (b): Data/MC reconstructed neutrino energy comparison of events selected by CC  $\nu_e$  cut set 6 with 4.4·10<sup>19</sup> POT of MicroBooNE run1 data. (c): MC-predicted CC  $\nu_e$  efficiency vs. true neutrino energy with CC  $\nu_e$  cut set 5 and 6, and the ratio of these two efficiency curves. Cut sets are defined in table IV.

At this stage, much of the remaining background is present due to photons or secondary showers being mis-classified as primary electrons or muons being mis-classified as charged pions (and therefore not getting rejected by the no reconstructed muons cut). The latter issue is addressed first.

Generally, when muon tracks are mis-classified as charged pions, they still get a fairly high LArPID muon score. Events remaining after "cut set 5" with a true muon present can therefore be identified by searching for those containing a track with a high muon score (even though events with muon-classified tracks have already been removed). Figure 25a shows the distribution for the log of the maximum LArPID muon score for any track attached to the candidate neutrino vertex in remaining events. The cut on this distribution that provides the largest CC  $\nu_e$  selection purity\*efficiency product is -3.7. Events with a track that has a muon score above this value were therefore removed as the new requirement in "cut set 6." The cut set 6 neutrino energy distributions and efficiency curves are shown in figure 25 (b) and (c). This cut does not have a large impact on selection efficiency.

The final cut seeks to remove events where a photon or a mis-reconstructed charged pion 1114 prong (composed of a charged pion and the electron produced in its decay) was mis-classifed 1115 by LArPID as a primary electron. As with the mis-classified muon tracks, in these cases, the 1116 network tends to hedge its bets and also give these showers a high photon or charged pion 1117 score. An electron class confidence metric for the candidate primary electron was therefore 1118 defined as the difference in its LArPID electron score and the average of its charged pion 1119 and photon scores:  $\log s_e - (\log s_{\pi} + \log s_{\gamma})/2$ , where  $s_e$ ,  $s_{\pi}$ , and  $s_{\gamma}$  are the electron, charged 1120 pion, and photon scores, respectively.<sup>6</sup> The distribution of the primary electron candidate's 1121 class confidence metric for signal and background events remaining after "cut set 6" is shown 1122 in figure 26a. The signal and background distributions separate out well. The electron class 1123 confidence cut that maximized the CC  $\nu_e$  purity\*efficiency product, class confidence > 7.1, 1124 was added as the final CC  $\nu_e$  selection cut. The data and MC reconstructed neutrino energy 1125 distributions with all selection cuts is shown in figure 26b, which includes a  $1\sigma$  uncertainty 1126 band on the predictions including both statistical and systematic (discussed in section IIIC) 1127 errors. As we will show in section IIID, the data and predictions are consistent within the 1128 quoted uncertainties. The final selection efficiency is shown in figure 26c along with a 1129 comparison to "cut set 6." Adding in the electron class confidence cut does significantly 1130 impact efficiency, but is necessary to remove remaining backgrounds. 1131

Additional cuts (including utilizing the LArPID completeness, purity, and production process score values) were tested, but none outperformed these results. With the cuts enumerated in table IV, we are able to achieve a CC  $\nu_e$  selection with an overall efficiency of 56.8% and purity of 91.1%, which is very competitive with PRD 105:112005 [17], the highest-efficiency CC  $\nu_e$  search previously published by MicroBooNE. Additional data/MC comparisons (including hand scans of selected data events), performance plots, and a detailed

<sup>&</sup>lt;sup>6</sup> We also attempted cutting separately on the charged pion and photon scores, but this did not achieve better results.

"Electron Class Confidence" for Largest Electron Shower



Figure 26: (a): MC and off-beam cosmic background data distributions of the candidate primary electron shower's electron class confidence (LArPID electron score minus average of charged pion and photon scores). The requirement that the primary electron candidate have an electron class confidence value above 7.1 was added to the final CC  $\nu_e$  cut set. (b): Data/MC reconstructed neutrino energy comparison of events selected by the full CC  $\nu_e$ cut set with  $4.4 \cdot 10^{19}$  POT of MicroBooNE run1 data. (c): MC-predicted CC  $\nu_e$  efficiency vs. true neutrino energy with all CC  $\nu_e$  cuts and cut set 6, and the ratio of these two efficiency curves. Cut sets are defined in table IV.

comparison of these results with the inclusive CC  $\nu_e$  selection of PRD 105:112005 are shown in section III D.

# 1140 B. CC numu inclusive selection cuts

Here, we use a similar approach - taking events with LArMatch-identified neutrino vertex
candidates (selecting the one with the highest score if there are multiple), applying the same
Wire-Cell cosmic rejection cuts discussed in section III A, and cutting on the LArPID outputs

of attached prongs - to achieve a highly effective inclusive CC  $\nu_{\mu}$  selection. Figure 22a from 1144 section III A shows the number of LArPID-identified muon tracks attached to the neutrino 1145 candidate for MC CC  $\nu_{\mu}$  events, cosmic, and (in this context) other simulated neutrino 1146 backgrounds (after applying Wire-Cell cosmic rejection cuts). A CC  $\nu_{\mu}$  dominated sample 1147 can be selected by simply requiring that there be at least one identified muon track attached 1148 to the LArMatch neutrino candidate vertex. (Note that figures 22b and 22c show results 1149 with the CC  $\nu_e$  requirement of 0 reconstructed muons, not the  $\geq 1$  condition discussed 1150 here for the CC  $\nu_{\mu}$  selection.) When there are multiple reconstructed muons in true CC  $\nu_{\mu}$ 1151 events, this is generally because of clustering errors in which a small section of the track 1152 is reconstructed as a separate cluster. In these cases, according to MC, the track with the 1153 highest LAPID muon score is truth-matched to the simulated muon 96.4% of the time, and 1154 the identified muon track with the most charge is matched to the true muon 95.7% of the 1155 time. 1156

This simple selection yields a predicted overall CC  $\nu_{\mu}$  purity of 96.0% and efficiency of 67.9%. While significant improvements were not achieved by applying further cuts on the LArPID outputs of the identified primary muon track or other attached prongs, we found that purity can be increased (at the expense of efficiency) by cutting on the neutrino keypoint score of the candidate neutrino vertex, the angle of the muon track (to remove downwards going cosmic-background muons), and the LArPID production process scores of the muon track.

The full set of CC  $\nu_{\mu}$  selection criteria are enumerated in table V. The predicted selection 1164 efficiency as a function of true neutrino energy after applying each cut is shown in figure 27b. 1165 As with the CC  $\nu_e$  selection, the largest impact on efficiency comes from the neutrino vertex 1166 reconstruction and the primary lepton identification. Distributions of reconstructed neutrino 1167 energy for data and MC (including the  $1\sigma$  uncertainty band calculated in section III C) with 1168 the full selection are shown in figure 27a. The overall data excess seen here is not unique 1169 to our CNN-based reconstruction and is consistent with the excess seen in the inclusive 1170 CC  $\nu_{\mu}$  selection of MicroBooNE's Wire-Cell reconstruction [17]. Furthermore, as we will 1171 show in section IIID, the data and predictions are consistent within quoted uncertainties. 1172 Additional data/MC comparisons and a more detailed comparison to the Wire-Cell CC  $\nu_{\mu}$ 1173 selection are presented in section IIID as well. 1174

Cut	Notes		
LArMatch-identified neutrino candidate vertex found inside	Added in cut set 1 (in-		
the fiducial volume	cluded in all cut sets)		
3D space points of prongs attached to neutrino candidate do not all overlap with Wire-Cell-tagged cosmics	Added in cut set 2 (in- cluded in final set as well)		
At least one track attached to the candidate neutrino vertex was identified by LArPID as a muon	Added in final cut set		

Table V: Inclusive CC  $\nu_{\mu}$  Selection Cuts



Figure 27: (a): Data/MC reconstructed neutrino energy comparison of events selected by the full CC  $\nu_{\mu}$  cut set with  $4.4 \cdot 10^{19}$  POT of MicroBooNE run1 data. (b): MC-predicted CC  $\nu_{\mu}$  efficiency vs. true neutrino energy after adding each CC  $\nu_{\mu}$  cut, along with a ratio of the full cet set and cut set 2 efficiency curves. Cut sets are defined in table V.

# 1175 C. Systematic uncertainty estimates

Modeling uncertainties that contribute to our systematic errors come from four main 1176 sources: modeling of the neutrino flux, modeling of the MicroBooNE detector, modeling 1177 of neutrino-argon cross sections, and modeling of hadron-argon cross sections. To account 1178 for detector systematics, we modify a variety of detector parameters, re-simulate a neutrino 1179 sample for each variation, and analyze their impact on our predictions. This is discussed 1180 in more detail in section IIIC1. While these detector variations can change observables 1181 in any event, variations in the parameters associated with the other sources of systematic 1182 uncertainty simply alter the rate at which different events occur. These flux and cross section 1183 uncertainties can therefore be studied by re-weighting individual events without the need to 1184 re-simulate new neutrino samples. This method and our flux and cross section systematics 1185



Figure 28: Fractional uncertainties in each reconstructed neutrino energy bin for the inclusive (a) CC  $\nu_e$  selection and (b) CC  $\nu_{\mu}$  selection. Statistical uncertainties on the cosmic background + neutrino predictions; systematic uncertainties from our modeling of the detector, flux, neutrino-argon cross sections, and hadron-argon interactions; and the total combined uncertainty is shown. The use of a flat detector systematic uncertainty in the CC  $\nu_{\mu}$  selection above 1.4 GeV is discussed in section III C 1.

# are discussed in more detail in section III C 2.

The results of those studies is summarized in figure 28, which shows uncertainties in our predicted event counts in each reconstructed neutrino energy bin used in the inclusive CC  $\nu_e$ and CC  $\nu_{\mu}$  selections. Our total uncertainty in each bin is shown, along with contributions from the four sources of systematic uncertainty discussed above and statistical errors from our finite cosmic background and simulated neutrino samples.

## 1192 1. Detector Systematic Uncertainties

To account for uncertainties in detector modeling, we vary parameters associated with the light yield (LY), light attenuation, and Rayleigh scattering length; "wiremod" modifications to the amplitudes and widths of wire waveforms as a function of x position, (y,z) position, and angles  $\theta_{xx}$  and  $\theta_{yz}$  of particle trajectories; a variation in electron-ion recombination parameters ("recomb2"); and an alternative electric field inside the TPC from the space charge effect (SCE). See e.g. [14] for additional information on these variations.

For each variation, we re-simulate the same sample of Monte Carlo neutrino events and calculate a covariance matrix for each kinematic observable to quantify the bin-by-bin shift in event counts:  $F_{ij}^k = (N_i^k - N_i^{CV})(N_j^k - N_j^{CV})/(N_i^{CV}N_j^{CV})$ , where  $F^k$  is the fractional <sup>1202</sup> covariance matrix for the *k*th variation,  $N_i^k$  is the number of events in bin *i* of the simulation <sup>1203</sup> with variation *k*, and  $N_i^{CV}$  is the number of events in bin *i* for the central value simulation <sup>1204</sup> with default detector parameters. Overall  $1\sigma$  detector-related fractional uncertainties in <sup>1205</sup> each bin are then given by  $\sigma_i/N_i = \sqrt{\sum_k F_{ii}^k}$ .

The computational expense associated with re-simulating neutrino events for each vari-1206 ation presents a significant challenge in quantifying these detector systematics. The  $O(10^5)$ 1207 event samples used in this analysis provided inadequate statistics to provide a robust esti-1208 mate of detector uncertainties in certain regions. For each variation, two simulations were 1209 combined to predict event counts: one  $\nu_{\mu}$  dominated sample in which neutrinos are simulated 1210 in the same proportion estimated to occur in the beam, and one involving only the intrinsic 1211 CC  $\nu_e$  component. While the intrinsic  $\nu_e$  simulation provided adequate statistics for CC  $\nu_e$ 1212 predictions, roughly just 10 raw neutral current and  $\nu_{\mu}$  background events (there are small 1213 variations between the different simulated samples) from the former beam simulation passed 1214 our CC  $\nu_e$  selection. Statistical variations from this background prediction therefore caused 1215 large artificial fluctuations in our estimated detector systematic uncertainties. In the CC  $\nu_{\mu}$ 1216 selection, statistics are also very low in the high energy tails of the reconstructed neutrino 1217 energy and muon momentum distributions (see figure 29), again causing large fluctuations 1218 in estimated systematics in those regions. 1219



Figure 29: Monte Carlo statistical errors on events passing the CC  $\nu_{\mu}$  selection for the central value simulation used to estimate detector systematics, binned in reconstructed neutrino energy (a) and muon momentum (b).

We will address these statistical shortcomings prior to publishing these results by reprocessing one-order-of-magnitude larger samples for these detector variations. As a tem-

porary solution, we place a lower bound on our detector systematics with the following 1222 corrections. For the CC  $\nu_{\mu}$  selection, we combine events above 1.4 GeV in reconstructed 1223 neutrino energy and above 1.2 GeV/c in reconstructed muon momentum into a single bin for 1224 those respective distributions. When calculating our total uncertainty in bins above those 1225 thresholds (as in figure 28b), we use the flat high energy/momentum detector systematics 1226 obtained with this approach. For the CC  $\nu_e$  selection, we assume that the kinematic de-1227 pendence of  $N_i^k - N_i^{CV}$ , the central value vs. detector variation excess in each bin of all 1228 kinematic distributions, is the same for the NC and  $\nu_{\mu}$  backgrounds that pass the selection 1229 as it is for the CC  $\nu_e$  signal events that pass the selection. With this assumption, we estimate 1230 the predicted signal + background event counts by scaling the CC  $\nu_e$  signal distributions by 1231  $(N_s + N_b)/N_s$ , where  $N_s$  and  $N_b$  are the total number of signal and background events that 1232 pass the selection, respectively. 1233

Our total detector systematic uncertainties in each reconstructed neutrino energy bin of 1234 the inclusive CC  $\nu_e$  and CC  $\nu_{\mu}$  selections with and without the low-statistics corrections 1235 discussed above is shown in figure 30. The uncertainties without the corrections provide a 1236 lower bound for our estimated detector-related modeling errors, while the larger, statistical-1237 fluctuation-driven uncertainties without the corrections provide an upper bound. To avoid 1238 inflating our detector systematics as a result of low-statistics fluctuations and provide a 1239 more strict test on data / Monte Carlo consistency in our selection results (discussed in 1240 section IIID), we use the lower-bound detector uncertainties with the statistical corrections 1241 discussed above. The full fractional covariance matrix (binned in reconstructed neutrino 1242 energy) for all detector variations with these low-statistics corrections is shown in figure 31. 1243

#### 1244 2. Flux, Cross Section, and Hadron Re-Interaction Uncertainties

To calculate systematic uncertainties arising from flux, neutrino cross section, and hadron re-interaction predictions we employ the same method outlined in [14]. Flux uncertainties arise from three main sources: the properties of the magnetic focusing horn, hadron production in the target, and secondary hadron interactions. Neutrino cross-section uncertainties arise from a large number of parameters associated with each neutrino interaction mode and final state interactions that affect all modes. The hadron re-interaction uncertainty calculations consider variations in parameters associated with hadron-argon cross sections



Figure 30: Total detector variation uncertainties in each reconstructed neutrino energy bin of the inclusive (a) CC  $\nu_e$  and (b) CC  $\nu_{\mu}$  selections. Results are shown with and without the low-statistics corrections discussed in the text.



Figure 31: Fractional covariance matrices binned in reconstructed neutrino energy from all detector variations for the inclusive (a) CC  $\nu_e$  and (b) CC  $\nu_\mu$  selections.

for protons and charged pions. These uncertainties are accounted for by re-weighting events with each systematic parameter variation and comparing the modified reconstructed spectra with the nominal simulation. Additional details on the variations considered are provided in [14].

Given the reconstructed spectra with bin counts  $N_i$  for each set of varied parameters, a covariance matrix M can be constructed where the variance in bin counts (resulting from the parameter variations) is provided in the diagonal entries and the covariance between the counts in each pair of bins in the off-diagonal entries. The fractional covariance matrices  $F_{ij} = M_{ij}/(N_iN_j)$  including all flux, cross section, and hadron re-interaction variations for



Figure 32: Fractional covariance matrices binned in reconstructed neutrino energy from all flux, cross section, and hadron re-interaction variations for the inclusive (a) CC  $\nu_e$  and (b) CC  $\nu_\mu$  selections.

the reconstructed neutrino energy spectra in the inclusive CC  $\nu_e$  and CC  $\nu_{\mu}$  selections are shown in figure 32.

As shown in figure 28, cross section uncertainties provide the largest contribution to our model-based systematics. Flux uncertainties are substantial as well; they are roughly half the size of cross section uncertainties at lower energies and larger at higher energies. Hadron re-interaction systematics contribute very little to our overall uncertainty.

# 1267 D. Results

The performance of the inclusive CC  $\nu_e$  and CC  $\nu_{\mu}$  selections demonstrate the effectiveness of this new CNN-based reconstruction. Our predicted selection efficiencies and purities outperform PRD 105:112005 [17], the highest-efficiency result previously published by MicroBooNE. This comparison is shown in table VI.

For the inclusive CC  $\nu_e$  selection, our deep-learning based reconstruction provides significantly higher predicted purities (91% compared to 82%) and efficiencies (57% compared to 46%). This amounts to a predicted 24% increase in the number of CC  $\nu_e$  events selected with significantly lower background. As shown in figure 33a, an improvement in efficiency is achieved across all true neutrino energies (except in the lowest 100-200 MeV bin, in which there is no statistically significant difference). For the inclusive CC  $\nu_{\mu}$  selection, we achieve the same overall efficiency as PRD 105:112005 but with a reduced background (purity of 96% compared to 92% from PRD 105:112005). However, as shown in figure 33b, the two analyses provide different efficiencies at different neutrino energies, with our reconstruction yielding a higher efficiency below 1 GeV and the analysis of PRD 105:112005 providing a higher efficiency above 1.5 GeV.

	DL Reco	PRD 105:112005
CC $\nu_e$ Selection Efficiency	57%	46%
CC $\nu_e$ Selection Purity	91%	82%
CC $\nu_{\mu}$ Selection Efficiency	68%	68%
CC $\nu_{\mu}$ Selection Purity	96%	92%

Table VI: Inclusive CC  $\nu_e$  and CC  $\nu_{\mu}$  selection results for our deep-learning-based reconstruction and PRD 105:112005 [17].



Figure 33: The predicted CC  $\nu_e$  (a) and CC  $\nu_{\mu}$  (b) selection efficiency of our reconstruction and selection (DL Gen2) and that of PRD 105:112005 (Wire-Cell) [17] as a function of true neutrino energy.

In sections III A and III B, we showed predicted (using MC neutrino simulations plus data cosmic-ray background) and MicroBooNE open data distributions of reconstructed neutrino energy for selected inclusive CC  $\nu_e$  and CC  $\nu_{\mu}$  events. Figures 34 and 35 show the same data/MC comparisons for reconstructed primary lepton momentum and  $\cos(\theta_l)$ (where  $\theta_l$  is the angle between the primary lepton and the beam). Also included are the reconstructed neutrino energy distributions, along with predicted purity and efficiency as a function of reconstructed neutrino energies. For both selections, purities are high for all



Figure 34: Predicted and MicroBooNE open data distributions of events passing the CC  $\nu_e$  selection in (a) reconstructed neutrino energy, (c) reconstructed electron momentum, and (d) reconstructed  $\cos(\theta_e)$ , where  $\theta_e$  is the angle between the reconstructed electron shower and the beam. (b): The predicted efficiency (from MC) and purity (from MC and off-beam cosmic background data) of the CC  $\nu_e$  selection as a function of reconstructed neutrino energy.

energies, whereas efficiency drops more dramatically, as expected, at low energies where it is more difficult to separate signal from background.

To assess the consistency between the predictions made for these distributions with our deep-learning based reconstruction framework and observations from the MicroBooNE open data set, we employ a  $\chi^2$  goodness-of-fit test using the combined Neyman-Pearson (CNP)  $\chi^2$  test statistic [36] with the covariance matrix formalism:

$$\chi^2 = (M - \mu)^T \cdot V_{\text{full}}^{-1} \cdot (M - \mu) \tag{6}$$

where M and  $\mu$  are vectors of the observed and predicted event counts in each bin and  $V_{\text{full}}$ 



Figure 35: Predicted and MicroBooNE open data distributions of events passing the CC  $\nu_{\mu}$  selection in (a) reconstructed neutrino energy, (c) reconstructed muon momentum, and (d) reconstructed  $\cos(\theta_{\mu})$ , where  $\theta_{\mu}$  is the angle between the reconstructed muon track and the beam. (b): The predicted efficiency (from MC) and purity (from MC and off-beam cosmic background data) of the CC  $\nu_{\mu}$  selection as a function of reconstructed neutrino energy.

<sup>1297</sup> is the full covariance matrix in the CNP method:

$$V_{\rm full} = V_{\rm CNP}^{\rm stat} + V_{\rm pred}^{\rm sys} + V_{\rm flux}^{\rm sys} + V_{\rm xsec}^{\rm sys} + V_{\rm det}^{\rm sys}$$
(7)

This covariance matrix is constructed from the flux and neutrino-argon and hadron-argon cross section covariance matrices ( $V_{\text{flux}}^{\text{sys}}$  and  $V_{\text{xsec}}^{\text{sys}}$ ) discussed in section III C 2, the detector systematics covariance matrix ( $V_{\text{det}}^{\text{sys}}$ ) from section III C 1, a diagonal matrix containing the variance in each bin from uncertainties arising from the finite statistics used to make predictions ( $V_{\text{pred}}^{\text{stat}}$ ), and a diagonal matrix containing the CNP terms: ( $V_{\text{CNP}}^{\text{stat}}$ )<sub>ii</sub> = 3/(1/M<sub>i</sub> + 2/\mu<sub>i</sub>). As discussed in section III C 1, we altered the binning used to calculate  $V_{\text{det}}^{\text{sys}}$  (and therefore changed its dimensions) for the reconstructed neutrino energy and muon momentum distributions of the CC  $\nu_{\mu}$  selection by combining high energy/momentum bins. Here, when constructing  $V_{det}^{sys}$  in Eq. 7 for those distributions, we estimate the covariance between individual bins in the overflow region and bin *i* as the covariance between the overflow bin and bin *i*. This maintains the approach of section III C 1 to (temporarily, pending processing of higher statistics detector variation samples) address low statistics with lower-bound estimates that provide a stricter test for data/MC consistency tests.

By comparing the  $\chi^2$  from Eq. 6 with the distribution of a  $\chi^2$  with N degrees of freedom 1311 (where N is the number of bins), we can calculate a p-value for our observations (the prob-1312 ability of seeing the observed or a more extreme fluctuation) and assess data / Monte Carlo 1313 consistency. However, the Gaussian assumptions used in the covariance matrix formalism 1314 followed here break down at low statistics, where much of the Gaussian probability distri-1315 butions fall into the un-physical region of negative bin counts. While this is not an issue for 1316 the CC  $\nu_{\mu}$  selection where predicted bin counts are sufficiently high across all bins of each 1317 distribution, in the CC  $\nu_e$  selection, predicted bin counts are almost all below 10 and fall 1318 below 1 in the tails. To make the CC  $\nu_e$  statistics closer to the Gaussian assumption, we 1319 combine all bins with a predicted event count below 2 for these goodness-of-fit tests. The re-1320 binned CC  $\nu_e$  distributions and the full covariance matrices (equation 7) for all distributions 1321 in both selections can be found in appendix A. 1322

The  $\chi^2$  and associated p-values calculated with this method for the reconstructed neutrino energy, lepton momentum, and lepton  $\cos(\theta)$  distributions for both selections is shown in table VII. All p-values are high: close to or above 90% for most tests and no lower than 24.4%. This indicates that the open data observations are consistent with our predictions and is evidence, for the kinematic variables considered, of a lack of any concerning data / Monte Carlo domain shift introduced by our deep-learning based reconstruction algorithms.

	$CC \nu_e$	$CC \nu_e$	$CC \nu_e$	$CC \nu_{\mu}$	$CC \nu_{\mu}$	$CC \nu_{\mu}$
	Selection,	Selection,	Selection,	Selection,	Selection,	Selection,
	$E_{\nu}$ Binning	$p_{e^-}$ Binning	$\cos(\theta)$ Binning	$E_{\nu}$ Binning	$p_{\mu}$ Binning	$\cos(\theta)$ Binning
$\chi^2/\text{DOF}$	3.80/9	3.06/8	5.18/6	25.08/21	11.91/21	9.73/16
p value	0.924	0.931	0.521	0.244	0.942	0.880

Table VII: Goodness of fit test results:  $\chi^2$  / degrees of freedom and associated p values for the reconstructed neutrino energy, lepton momentum, and lepton  $\cos(\theta)$  distributions in the inclusive CC  $\nu_e$  and CC  $\nu_{\mu}$  selections.

#### 1329 E. Results of Data and MC comparison using Open Data Sample

To further test our predicted inclusive CC  $\nu_e$  selection results and comparison to PRD 1331 105:112005 [17], we manually hand scanned all MicroBooNE run1 open data events selected 1332 by our analysis and that of PRD 105:112005, classifying each as either CC  $\nu_e$  or background. 1333 This open data set contains  $4.4 \cdot 10^{19}$  POT of run 1 data.

In the analysis of PRD 105:112005, 40 events were selected, of which (according to our hand scans) 37 or 38 were true CC  $\nu_e$  interactions. In our analysis, 44 events were selected, of which 42 or 43 were true CC  $\nu_e$  interactions (there is some uncertainty in the hand scan classifications). These results, along with comparisons to predictions made in the previous section, are summarized in table VIII.

	DL Reco Data Hand Scan Estimate	DL Reco MC Prediction	PRD 105:112005 Data Hand Scan Estimate	PRD 105:112005 MC Prediction
Total Events	44	48.3	40	41.2
Signal Count	42 - 43	44.0	37 - 38	33.8
Background Count	1 - 2	4.3	2 - 3	7.3
Purity	95% - 98%	91%	93% - 95%	82%

Table VIII: Hand scan results of inclusive CC  $\nu_e$  events selected from the open data sample by our deep-learning-based reconstruction and PRD 105:112005 [17].

These results are generally consistent with our expectations, given the large statistical 1339 uncertainties with these small numbers of events. With 4 - 6 more probable signal events 1340 selected by our framework, these results support our prediction of an increase (compared 1341 to PRD 105:112005) in inclusive CC  $\nu_e$  selection efficiency. Additionally, while the total 1342 number of selected probable signal events was higher by 4 - 6, there were 11 probable signal 1343 events selected by our framework that were not present in the analysis of PRD 105:112005 1344 and 6 probable signal events found in PRD 105:112005 that did not appear in our selection. 1345 This indicates that combining the events selected by our framework and PRD 105:112005 1346 (which utilizes the Wire-Cell reconstruction [17-19]) could yield an even more substantial 1347 improvement in efficiency, a promising avenue for future work. 1348

The three hand-scan-classified CC  $\nu_e$  events lowest in reconstructed neutrino energy are shown in figures 36 - 38.



Figure 36: Wire plane images of a probable CC  $\nu_e$  event selected by our analysis from the MicroBooNE open data set.



Figure 37: Wire plane images of a probable CC  $\nu_e$  event selected by our analysis from the MicroBooNE open data set.

# 1351 IV. DISCUSSION

A new reconstruction workflow has been developed that utilizes three convolutional neural networks to perform pattern recognition relatively early in the reconstruction workflow. This leverages the powerful ability of CNNs to recognize features in low-level data, specifically, the image-like data produced by the LArTPC wire planes. The many outputs and the ability to partition the spacepoints into topological classes greatly simplified the reconstruction of 3D spacepoints. Though this is also in part due to the energy range of interactions for



Figure 38: Wire plane images of a probable CC  $\nu_e$  event selected by our analysis from the MicroBooNE open data set.

MicroBooNE. With median energies below 1 GeV, the final state particles emerging from 1358 neutrino interactions often do not overlap. Final state particles more often than not emerge 1359 from the vertex at well-separated angles – which adds to the advantage working in 3D space 1360 has for clustering. However, we believe the utility of feature recognition by 2D CNNs are on 1361 display given the modest complexity of the non-DL algorithms implemented in this work. 1362 Furthermore, the particular use of the LAPID CNN mitigates the impact of mistakes made 1363 in the 3D reconstruction. This comes from the use of information about both the particle 1364 under consideration and the entire image of the interaction. We believe one lesson that 1365 should carry over to analyses being built for future LATTPCs like SBND and DUNE, is that 1366 access to the 2D image information will have much utility. 1367

The quality of the reconstruction and the utility of the CNN outputs were tested through 1368 the exercise of selecting inclusive charged-current  $\nu_{\mu}$  and  $\nu_{e}$  interactions. We looked for 1369 potentially large, show-stopping domain shift effects by testing the selection on the Micro-1370 BooNE open dataset. The cuts employed are deceptively simple in that they are flat cuts on 1371 particle ID scores or on the numbers of certain particles. They are deceptively simple, be-1372 cause in other MicroBooNE selections BDTs, using a collection of kinematic observables and 1373 spatial patterns, was often required to reach the best efficiency and/or purity. However, the 1374 CNNS used in this work, we conjecture, likely utilizes the same kinematic correlations ex-1375 tracted directly from the 2D images and contributes to the improvement in  $\nu_e$ -CC efficiency 1376 across a large range of true neutrino energies. 1377
Interestingly, this improvement in the  $\nu_e$ -CC selection constrasts with the roughly equal 1378 performance between this work and the inclusive  $\nu_{\mu}$ -CC selection of PRD 105:112005 [17] 1379 utilizing the Wire-Cell reconstruction. In the CC  $\nu_e$  selection, we leverage the LArPID 1380 scores to further reduce backgrounds by vetoing events with an identified muon or cutting 1381 events with sufficient evidence that the primary shower either derived from charged pions 1382 or is a photon. For the inclusive  $CC\nu_{\mu}$  event selection, there was not a set of single particles 1383 associated strongly with potential background interactions. Instead, improvement in the 1384 signal acceptance or rejection of background will likely need to come through the use of 1385 correlations between particle kinematics or tuning of cuts in different regions of kinematic 1386 phase space. We leave explorations to improve the selections using the reconstructed particle 1387 kinematics to future work. For now, our conjecture is that the inclusive  $CC\nu_{\mu}$  selection is 1388 primarily defined by the upstream Wire-Cell cosmic tagging algorithms. The fact that our 1389 efficiency and purity are similar possibly reflects a similar ability to identify the muon within 1390 the in-time charge cluster. 1391

Further conjecture is based in part on the last two cuts applied in the  $\nu_e$ -CC selection. 1392 These cuts can be interpreted as examples of how CNNs utilize fine image details to great 1393 effect. The last two cuts both target the separation of primary electrons from secondary 1394 electrons coming from the decay of a low-energy muon or charged pion. In these cases, the 1395 information to complete the tasks is located in small regions of the image: the beginning of 1396 showers and around the vertex. The utilization of this information is what we hypothesize 1397 to be the source of the efficiency and purity gains. For example, there can be difficult edges 1398 cases when estimating dE/dx for particle ID. One such case are the potential presence of 1399 additional particles near the vertex. These particles can be of a low enough energy such 1400 that they are missed by the reconstruction, but high enough in energy to impact estimates 1401 like the dE/dx for identified trajectories. Specific scenarios include a short co-linear proton 1402 or a localized region of high energy deposition from a Brem photon emitted early in the 1403 trunk of the shower. Both can push a dE/dx estimate to mis-identify an electron shower 1404 as photon. We conjecture that the LArPID network is able to learn a set of image features 1405 that can detect these edge cases and influence the electron PID. Demonstrating this is one 1406 area for future study. But one piece of circumstantial evidence is the lack of dependence 1407 on the energy scale of the neutrino interaction. In this hypothesis, the occurrence of such 1408 scenarios are broadly distributed across the range of neutrino energies. The possible lack of 1409

comparable scenarios for identifying muons would then explain why improvements are not observed for the  $\nu_{\mu}$  selection.

Inspecting the distributions of the LArPID score for the  $\nu_e$  selection in figure 26, the most 1412 similar distribution to the CCnumu events that remain are the NCnumu events. Cosmic 1413 interactions also peak in a similar region. As discussed above, the electron confidence score 1414 was developed to ID interactions with evidence that the candidate electron shower is actually 1415 a secondary electron from a decay muon or charged pion. For NC events with true neutrino 1416 energies near the peak of 800 MeV, the final state momentum for the charged pions is 1417 likely small. Alternatively, a charged pion with an early decay in flight leads to what 1418 is now easily misinterpretable as an event with a primary muon in the final state. But 1419 in addition to such visual evidence, the LArPID CNN likely has learned to use particle 1420 kinematics better separate CC  $\nu_e$  events from the various backgrounds. Such kinematic 1421 information is also the kind of information that would be effectively exploited by a BDT-1422 based selection – as was used in the 2022 inclusive search of PRD 105:112005 [17]. At the 1423 high-level observable distributions studied, we do not find evidence that the CNN-based 1424 reconstruction and selection are more sensitive to argon-interaction modeling uncertainties 1425 when compared to past analyses. But future work will focus on how to dig deeper into this 1426 potential bias. 1427

However, as with all machine learning methods, we must vet the CNNs presumed ability 1428 to correlate latent physical quantities or scenarios to distributions over possible images. 1429 The goal of this work is to report on the completed workflow, and provide evidence of its 1430 competitiveness to past analyses. But more work is ongoing to evaluate the robustness of 1431 this analysis centered on CNNs. The model learning to recognize the features discussed 1432 above derives from training on our simulation data. This data is produced using models 1433 of the MicroBooNE detector and physics like the ionization produced by charged particles. 1434 Though not perfect, one might hypothesize that the level of detector mis-modeling here is 1435 at a manageable level. This is supported by the level of change in the number of selected 1436 events. Even with the higher bound estimates, which we believe are likely due to low MC 1437 statistics, the uncertainties from detector-related effects are similar to the analysis of PRD 1438 105:112005 [17]. Future work can also be done to directly address certain aspects of this 1439 type of domain shift such as adversarial training. 1440

While the gains in the  $\nu_e$  might come from what has been discussed, the context im-

ages also allow the use of correlations between particle frequency and particle kinematics. 1442 The underlying correlations in the training data, in this case, come from neutrino-argon 1443 interaction modeling, which has uncertainties larger relative to the physics discussed before. 1444 Future work will aim at understanding the degradation of performance of the LArPID net-1445 work when confronted with images that contain particles with kinematic correlations some 1446 distance outside of the support of the training data. This means that wildly out-of-domain 1447 examples could simply be ignored by the models. Developments in anomaly detection are 1448 one of several directions to research how to improve model robustness or detect issues re-1449 lated to exotic final states or unusual particle kinematics. There is also the area of domain 1450 adaption which aims to find ways to improve robustness. 1451

CNN models, such as the LArMatch keypoint model, will also be impacted by the use 1452 of training images simulating a LArTPC at the surface. In such a detector, there will be a 1453 high rate of cosmic interactions in each image. For MicroBooNE, this was approximately 1454 10-15 interactions. Generally, our cosmic simulations left more interactions per image than 1455 was seen in the data. Mismodeling cosmic interaction rates are important for several back-1456 grounds, in particular to interactions with low-energy showers. Such backgrounds include 1457 stopping muons entering near the cathode and leaving a short track and Michel electron, 1458 entering photons, and those produced from hadronic interactions, e.g. from the decay of 1459 neutral pions. As a potential impact, the neutrino vertex finder scores in this context could 1460 be sensitive to the relative rate of neutrino-induced and cosmogenic single-shower events. 1461

Another topic of discussion is what the potential impact this work might have in the future for both DL and non-DL reconstruction in LArTPCs. For one, the LArPID strategy of using contextual information around a defined cluster is readily adaptable to existing MicroBooNE Pandora and Wire-Cell analyses. One might speculate that the differences in what amounts to the LArPID image pre-processing step for the particle cluster image will have a limited impact on the LArPID behavior. Future work includes plans to investigate LArPID integration into these existing workflows.

Many of the hand-engineered algorithms in this work are very simple in their core approaches, but might require heuristics to tune their behaviors and/or handle edge cases. This leads to several parameters per algorithm and an overall large number of parameters affecting the behavior of the reconstruction. Such parameters for each algorithm were tuned during development on a relatively small MC sample size, O(100) events, in order to iter-

ate and tune these parameters on a day-length time-scale. In contrast, for the DL-based 1474 reconstruction framework in Ref. [11] (referred to as "mlreco3d"), these algorithms have 1475 ML-based counterparts which one might expect to perform better just due to the simple 1476 fact that the algorithms are learned by optimizing them over the entire available training 1477 data. The mlreco3d framework centers around a 3D voxel representation of the LArTPC 1478 data, similar to the use of spacepoints in this work. In particular, the task of forming 1479 subclusters and then collecting them into particle candidates is addressed through the use 1480 of graph neural networks (GNNs). GNNs are likely much more accurate than our shower 1481 reconstruction, which is merely a simple cone-based aggregator. Indeed, the purity versus 1482 completion plots for the electron clusters are the least accurate for our workflow. Similarly, 1483 in mlreco<sup>3</sup>d associations of particle candidates to potential neutrino interactions are also 1484 done with graphs. Furthermore, mlreco3d's determination of keypoints and voxel-wise par-1485 ticle labels make use of the 3D structure in a more direct way than in LArMatch, which 1486 relies only on 2D image features correlated across the wire planes. 1487

In contrast to the 3D spacepoint algorithms, the CNN components in our work would 1488 be the component that would best integrate with a fully ML framework such as mlreco3d. 1480 Indeed, the LArMatch real/ghost classifier was developed to provide a CNN-based pre-1490 processing step leading into the mlreco3d pipeline. One direction is to investigate if im-1491 provements could be made by injecting the spacepoint feature vectors into key parts of the 1492 mlreco3d framework. Because the pipeline fully leaves behind the 2D low-level data, one 1493 might believe that LArMatch's image feature vector can be used to preserve useful details 1494 otherwise lost when moving the representation of the data from 2D images into 3D voxels. 1495 Furthermore, one would also expect that individual particle clustering will not be perfect. 1496 And, therefore, a LArPID-like stage will be useful in similar ways to the reconstruction and 1497 selection described in this work. 1498

## 1499 V. CONCLUSIONS

This work represents a milestone in the development of ML tools for LArTPC analysis. We demonstrate – for the first time on real LArTPC data – a deep-learning based generic neutrino interaction reconstruction framework that is competitive with the current stateof-the-art: The inclusive CC  $\nu_e$  and CC  $\nu_{\mu}$  selections obtained with the outputs of our

reconstruction compare favorably to the highest-efficiency results previously published by 1504 MicroBooNE [17], with reduced backgrounds and a predicted 24% increase in the number 1505 of selected CC  $\nu_e$  events. Hand scans of selected CC  $\nu_e$  events from a small MicroBooNE 1506 open data set are consistent with these predictions. These results demonstrate the power 1507 of CNNs to leverage the full set of information provided in LArTPC wire-plane images 1508 at multiple stages of the framework: in low-level reconstruction of vertices and 3D space 1509 points (LArMatch), tagging pixels as track or shower like to aid in downstream clustering 1510 algorithms (SSNet), and analyzing reconstructed 3D prongs with the aid of full wire-plane 1511 images to fold in-context information that may have been lost by inaccuracies in upstream 1512 algorithms (LArPID). 1513

A possible downside of our approach stems from the black-box nature of these deep 1514 networks and their potential to introduce biases from the use of supervised learning on sim-1515 ulated data. While a more thorough investigation of network-based systematic uncertainties 1516 and model interpretation studies will be the subject of future work, we have demonstrated 1517 that simulated MC distributions of high-level reconstructed kinematic variables for selected 1518 charged-current neutrino interactions are consistent with data. This provides evidence of 1519 the robustness of our framework and a lack of highly significant data/MC domain shifts 1520 introduced by the use of CNNs trained on simulated data. 1521

These results show promise for the deep-learning based reconstruction tools developed 1522 here to improve the sensitivity of LArTPC physics analyses. Future studies will employ this 1523 reconstruction framework in cross-section measurements and new physics searches. In the 1524 near term, individual tools within the framework could be quickly integrated into alternative 1525 reconstruction packages. The LArPID network, for example, could easily be run over 3D 1526 tracks and showers reconstructed by Wire-Cell or other frameworks. As the use of such tools 1527 in high energy physics analyses proliferates, this work contributes towards understanding the 1528 power and robustness of computer vision techniques when applied to LArTPC neutrino data. 1529 It also points towards the improvements these methods can make on the physics that will 1530 come out of future LArTPC experiments, specifically from the short-baseline experiments 1531 over the next few years. 1532

- [1] R Acciarri et al. (MicroBooNE Collaboration). Design and construction of the microboone
   detector. Journal of Instrumentation, 12(02):P02017, 2017. URL https://dx.doi.org/10.
   1088/1748-0221/12/02/P02017.
- [2] R Acciarri et al. (ICARUS-WA104, LAr1-ND, and MicroBooNE Collaborations). A proposal
   for a three detector short-baseline neutrino oscillation program in the fermilab booster neutrino
   beam. arXiv:1503.01520, 2015. URL https://doi.org/10.48550/arXiv.1503.01520.
- [3] S Amerio et al. (ICARUS Collaboration). Design, construction and tests of the icarus t600
   detector. Nuclear Instruments and Methods in Physics Research Section A: Accelerators,
   Spectrometers, Detectors and Associated Equipment, 527(3):329-410, 2004. URL https://
   doi.org/10.1016/j.nima.2004.02.044.
- [4] B Abi et al. (DUNE Collaboration). Volume i. introduction to dune. Journal of Instrumenta *tion*, 15(08):T08008, 2020. URL https://dx.doi.org/10.1088/1748-0221/15/08/T08008.
- [5] B Abi et al. (DUNE Collaboration). The single-phase protodune technical design report.
   arXiv:1706.07081, 2017. URL https://doi.org/10.48550/arXiv.1706.07081.
- [6] D A Dwyer, M Garcia-Sciveres, D Gnani, C Grace, S Kohn, M Kramer, A Krieger, C J Lin,
  K B Luk, P Madigan, C Marshall, H Steiner, and T Stezelberger. Larpix: Demonstration of
  low-power 3d pixelated charge readout for liquid argon time projection chambers. *Journal of Instrumentation*, 13(10):P10007, 2018. URL https://dx.doi.org/10.1088/1748-0221/13/
  10/P10007.
- [7] R Acciarri et al. (MicroBooNE Collaboration). Convolutional neural networks applied to
   neutrino events in a liquid argon time projection chamber. *Journal of instrumentation*, 12
   (03):P03011, 2017. URL https://dx.doi.org/10.1088/1748-0221/12/03/P03011.
- [8] B Abi et al. (DUNE Collaboration). Neutrino interaction classification with a convolutional
   neural network in the dune far detector. *Physical Review D*, 102(9):092003, 2020. URL
   https://doi.org/10.1103/PhysRevD.102.092003.
- [9] Kiara Carloni, Nicholas W Kamp, Austin Schneider, and Janet M Conrad. Convolutional neural networks for shower energy prediction in liquid argon time projection chambers. *Journal* of Instrumentation, 17(02):P02022, 2022. URL https://dx.doi.org/10.1088/1748-0221/ 17/02/P02022.

- [10] Pierre Baldi, Jianming Bian, Lars Hertel, and Lingge Li. Improved energy reconstruction in
   nova with regression convolutional neural networks. *Physical Review D*, 99(1):012011, 2019.
   URL https://doi.org/10.1103/PhysRevD.99.012011.
- [11] François Drielsma, Kazuhiro Terao, Laura Dominé, and Dae Heun Koh. Scalable,
   end-to-end, deep-learning-based data reconstruction chain for particle imaging detectors.
   *arXiv:2102.01033*, 2021. URL https://doi.org/10.48550/arXiv.2102.01033.
- [12] C Adams et al. (MicroBooNE Collaboration). Deep neural network for pixel-level electromag netic particle identification in the microboone liquid argon time projection chamber. *Physical Review D*, 99(9):092001, 2019. URL https://doi.org/10.1103/PhysRevD.99.092001.
- [13] P Abratenko et al. (MicroBooNE Collaboration). Semantic segmentation with a sparse con volutional neural network for event reconstruction in microboone. *Physical Review D*, 103(5):
   052012, 2021. URL https://doi.org/10.1103/PhysRevD.103.052012.
- [14] P Abratenko et al. (MicroBooNE Collaboration). Search for an anomalous excess of charged current quasielastic ν<sub>e</sub> interactions with the microboone experiment using deep-learning-based
   reconstruction. *Physical Review D*, 105(11):112003, 2022. URL https://doi.org/10.1103/
   PhysRevD.105.112003.
- [15] P Abratenko et al. (MicroBooNE Collaboration). Search for an excess of electron neutrino
   interactions in microboone using multiple final-state topologies. *Physical review letters*, 128
   (24):241801, 2022. URL https://doi.org/10.1103/PhysRevLett.128.241801.
- [16] A A Aguilar-Arevalo et al. (MiniBooNE Collaboration). Updated miniboone neutrino oscil lation results with increased data and new background studies. *Physical Review D*, 103(5):
   052002, 2021. URL https://doi.org/10.1103/PhysRevD.103.052002.
- <sup>1584</sup> [17] P Abratenko et al. (MicroBooNE Collaboration). Search for an anomalous excess of inclu-<sup>1585</sup> sive charged-current  $\nu_e$  interactions in the microboone experiment using wire-cell reconstruc-<sup>1586</sup> tion. *Phys. Rev. D*, 105:112005, Jun 2022. URL https://doi.org/10.1103/PhysRevD.105. <sup>1587</sup> 112005.
- [18] P Abratenko et al. (MicroBooNE Collaboration). Wire-cell 3d pattern recognition techniques
   for neutrino event reconstruction in large lartpcs: algorithm description and quantitative
   evaluation with microboone simulation. Journal of instrumentation, 17(01):P01037, 2022.
   URL https://dx.doi.org/10.1088/1748-0221/17/01/P01037.
- <sup>1592</sup> [19] P Abratenko et al. (MicroBooNE Collaboration). Cosmic ray background rejection with wire-

- cell lartpc event reconstruction in the microboone detector. *Physical Review Applied*, 15:
   064071, 2021. URL https://doi.org/10.1103/PhysRevApplied.15.064071.
- [20] R Acciarri et al. (MicroBooNE Collaboration). Noise characterization and filtering in the
   microboone liquid argon tpc. Journal of Instrumentation, 12(08):P08003, 2017. URL https:
   //dx.doi.org/10.1088/1748-0221/12/08/P08003.
- [21] C Adams et al. (MicroBooNE Collaboration). Ionization electron signal processing in single
   phase lartpcs. part i. algorithm description and quantitative evaluation with microboone simulation. Journal of Instrumentation, 13(07):P07006, 2018. URL https://dx.doi.org/10.
   1088/1748-0221/13/07/P07006.
- [22] C Adams et al. (MicroBooNE Collaboration). Ionization electron signal processing in single
   phase lartpcs. part ii. data/simulation comparison and performance in microboone. Journal
   of Instrumentation, 13(07):P07007, 2018. URL https://dx.doi.org/10.1088/1748-0221/
   13/07/P07007.
- [23] Olaf Ronneberger, Philipp Fischer, and Thomas Brox. U-net: Convolutional networks
   for biomedical image segmentation. In Medical Image Computing and Computer-Assisted
   Intervention-MICCAI 2015: 18th International Conference, Munich, Germany, October 5-9,
   2015, Proceedings, Part III 18, pages 234-241. Springer, 2015. URL https://link.springer.
   com/chapter/10.1007/978-3-319-24574-4\_28.
- <sup>1611</sup> [24] K He, X Zhang, S Ren, and J Sun. Deep residual learning for image recognition.
   arXiv:1512.03385, 2015. URL https://doi.org/10.48550/arXiv.1512.03385.
- [25] Dmitry Ulyanov, Andrea Vedaldi, and Victor Lempitsky. Instance normalization: The missing
   ingredient for fast stylization. arXiv:1607.08022, 2016. URL https://doi.org/10.48550/
   arXiv.1607.08022.
- [26] Benjamin Graham and Laurens Van der Maaten. Submanifold sparse convolutional networks.
   *arXiv:1706.01307*, 2017. URL https://doi.org/10.48550/arXiv.1706.01307.
- [27] JunYoung Gwak, Christopher B Choy, and Silvio Savarese. Generative sparse detection net works for 3d single-shot object detection. arXiv:2006.12356, 2020. URL https://doi.org/
   10.48550/arXiv.2006.12356.
- [28] Tsung-Yi Lin, Priya Goyal, Ross Girshick, Kaiming He, and Piotr Dollár. Focal loss for
   dense object detection. In *Proceedings of the IEEE international conference on computer vi-*
- sion, pages 2980-2988, 2017. URL https://doi.ieeecomputersociety.org/10.1109/ICCV.

1624 2017.324.

- [29] P Abratenko et al. (MicroBooNE Collaboration). Vertex-finding and reconstruction of con tained two-track neutrino events in the microboone detector. Journal of instrumentation, 16
   (02):P02017, 2021. URL https://dx.doi.org/10.1088/1748-0221/16/02/P02017.
- [30] R L Workman et al. Review of Particle Physics. *PTEP*, 2022:083C01, 2022. doi:
   10.1093/ptep/ptac097.
- [31] P Abratenko et al. (MicroBooNE Collaboration). Electromagnetic shower reconstruction and
   energy validation with michel electrons and π<sup>0</sup> samples for the deep-learning-based analyses in
   microboone. Journal of Instrumentation, 16(12):T12017, 2021. URL https://dx.doi.org/
   10.1088/1748-0221/16/12/T12017.
- [32] F Psihas, E Niner, M Groh, R Murphy, A Aurisano, A Himmel, K Lang, M D Messier,
   A Radovic, and A Sousa. Context-enriched identification of particles with a convolutional
   network for neutrino events. *Physical Review D*, 100:073005, 2019. URL https://doi.org/
   10.1103/PhysRevD.100.073005.
- [33] A Kendall, Y Gal, and R Cipolla. Multitask learning using uncertainty to weigh losses for
   scene geometry and semantics. arXiv:1705.07115, 2018. URL https://doi.org/10.48550/
   arXiv.1705.07115.
- [34] I Loshchilov and F Hutter. Decoupled weight decay regularization. arXiv:1711.05101, 2019.
   URL https://doi.org/10.48550/arXiv.1711.05101.
- [35] L N Smith and N Topin. Super-convergence: Very fast training of neural networks using
   large learning rates. arXiv:1708.07120, 2018. URL https://doi.org/10.48550/arXiv.
   1708.07120.
- [36] Xiangpan Ji, Wenqiang Gu, Xin Qian, Hanyu Wei, and Chao Zhang. Combined ney man-pearson chi-square: An improved approximation to the poisson-likelihood chi-square.
   *Nuclear Instruments and Methods in Physics Research Section A*, 961:163677, 2020. URL
- 1649 https://doi.org/10.1016/j.nima.2020.163677.

## 1650 Appendix A: Additional distributions for data vs expectation comparisons

In this appendix, we show the re-binned kinematic variable distributions for the CC  $\nu_e$ selection (figure 39) and the full covariance matrices (figure 40) used for the  $\chi^2$  goodness of fit tests discussed in section III D.



Figure 39: Predicted and MicroBooNE open data distributions, with the binning used in the  $\chi^2$  goodness of fit tests of section IIID, of events passing the CC  $\nu_e$  selection binned in (a) reconstructed neutrino energy, (b) reconstructed electron momentum, and (c) reconstructed  $\cos(\theta_e)$ , where  $\theta_e$  is the angle between the reconstructed electron shower and the beam.



Figure 40: The full fractional covariance matrices used in the  $\chi^2$  goodness of fit tests from section III D.